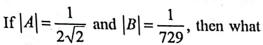
1. Let A and B be matrices of order  $3\times3$ .



is the value of |2B(adj(3A))|?



(b) 
$$\frac{27}{2\sqrt{2}}$$

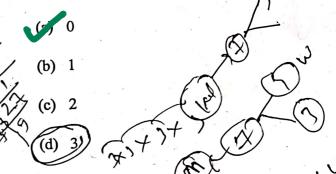
(c) 
$$\frac{27}{2}$$

- **(1)** 1
- 2. If z is any complex number and  $iz^3 + z^2 z + i = 0$ , where  $i = \sqrt{-1}$ , then what is the value of  $(|z|+1)^2$ ?

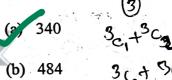


- (c) 81
- (d) 121
- 3. What is the sum of all four digit numbers formed by using all digits 0, 1, 4, 5 without repetition of digits?
  - (a) 44440
  - (b) 46460
  - (c) 46440
  - (3) 64440

4. If x, y and z are the cube roots of unity, then what is the value of xy + yz + zx 3



5. A man has 7 relatives (4 women and 3 men). His wife also has 7 relatives (3 women and 4 men). In how many ways can they invite (3) women and (3) men so that (3) of them are man's relatives and 3 of them are his wife's relatives?



- (c) 485
- 2(d) 469
- 6. A triangle PQR is such that 3 points lie on the side PQ, 4 points on QR and 5 points on RP respectively. Triangles are constructed using these points as vertices. What is the number of
  - (a) 205

triangles so formed?

- (b) 206
- (c) 215
- (d) 220

7. If  $log_b a = p$ ,  $log_d c = 2p$  and  $log_f e = 3p$ , then what is  $(ace)^{\frac{1}{p}}$  equal to ?



- bdf bdf
- (c)  $b^3d^2f$
- (d)  $b^2 d^2 f^2$
- 8. If  $-\sqrt{2}$  and  $\sqrt{3}$  are roots of the equation  $a_0 + a_1x + a_2x^2 + a_3x^3 + x^4 = 0$  where  $a_0$ ,  $a_1$ ,  $a_2$ ,  $a_3$  are integers, then which one of the following is correct?

(a) 
$$a_2 = a_3 = 0$$

(b) 
$$a_2 = 0$$
 and  $a_3 = -5$ 

(c) 
$$a_0 = 6$$
,  $a_3 = 0$ 

(d) 
$$a_1 = 0$$
 and  $a_2 = 5$ 

9. Let  $z_1$  and  $z_2$  be two complex numbers such that  $\left| \frac{z_1 + z_2}{z_1 - z_2} \right| = 1$ , then what is

$$Re\left(\frac{z_1}{z_2}\right) + 1$$
 equal to?

- (a) -1
- (b) 0

(2) 1

(d) 5

10. If  $26! = n8^k$ , where k and n are positive integers, then what is the maximum value of k?

(a) 6



(d) 9

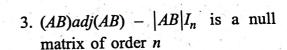


11. Consider the following statements in respect of two non-singular matrices A and B of the same order n:

5 B Crack

1. 
$$adj(AB) = (adjA)(adjB)$$

$$2. adj(AB) = adj(BA)$$



How many of the above statements are correct?

- (a) None
- Only one statement
  - (c) Only two statements
  - (d) All three statements

- 12. Consider the following statements in respect of a non-singular matrix  $\Lambda$  of order n:
  - 1.  $A(adjA^T) = A(adjA)^T$
  - 2. If  $A^2 = A$ , then A is identity matrix of order n
  - 3. If  $A^3 = A$ , then A is identity matrix of order n

Which of the statements given above are correct?

- (a) 1 and 2 only
  - (b) 2 and 3 only
  - (c) 1 and 3 only
- (a) 1, 2 and 3
- 13. How many four-digit natural numbers are there such that all of the digits are even?
  - (a) 625
  - (b) 500
  - (c) 400
  - (d) 256
- 14. If  $\omega \neq 1$  is a cube root of unity, then what are the solutions of  $(z-100)^3 + 1000 = 0$ ?
  - (a)  $10(1-\omega)$ ,  $10(10-\omega^2)$ , 100
  - (25)  $10(10-\omega)$ ,  $10(10-\omega^2)$ , 90

- (c)  $10(1-\omega)$ ,  $10(10-\omega^2)$ , 1000
- (d)  $(1 + \omega)$ ,  $(10 + \omega^2)$ , -1

15. What is  $(1+i)^4 + (1-i)^4$  equal to, where  $i = \sqrt{-1}$ ?

(a) 4 (b) 0

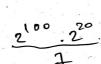
- (1) -8
- 16. Consider the following statements in respect of a skew-symmetric matrix A of order 3:
  - 1. All diagonal elements are zero.
  - 2. The sum of all the diagonal elements of the matrix is zero.
  - 3. A is orthogonal matrix.

Which of the statements given above are correct?

1 and 2 only

- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

- 17. Four digit numbers are formed by using the digits 1, 2, 3, 5 without repetition of digits. How many of them 1,7,3,5 (WP) are divisible by 4?
  - (a) 120
  - (b) 24
  - (c) 12
- 18. What is the remainder when  $2^{120}$  is divided by 7?



- (c) 5

(b) 3

- (d) 6
- 19. For what value of n is the determinant

$$\begin{vmatrix} C(9,4) & C(9,3) & C(10,n-2) \\ C(11,6) & C(11,5) & C(12,n) \\ C(m,7) & C(m,6) & C(m+1,n+1) \end{vmatrix} = 0$$

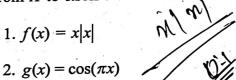
for every m > n?

(a) 4 (b) 5

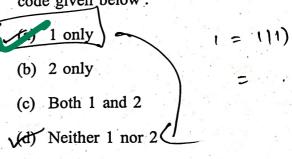


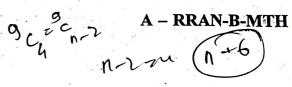
20. If ABC is a triangle, then what is the value of the determinant

- (d) 3
- 21. What is the number of different, matrices, each having 4 entries that can be formed using 1, 2, 3, 4 (repetition is Pallowed)?
- (a) 72 (b) 216
- 22. Let  $A = \{x \in R: (-1 < x < 1)\}$  Which of the following is/are bijective functions from A to itself?  $\equiv$

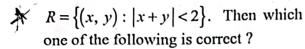


Select the correct answer using the code given below:





23. Let R be a relation on the open interval (-1, 1) and is given by



- (a) R is reflexive but neither symmetric nor transitive
- (b) R is reflexive and symmetric but not transitive
- (c) R is reflexive and transitive but not symmetric
- R is an equivalence relation

24. For any three non-empty sets A, B, C, what is

$$(A \cup B) - \{(A - B) \cup (B - A) \cup (A \cap B)\}$$

# equal to?







(d) 
$$(A \cup B) - (A \cap B)$$

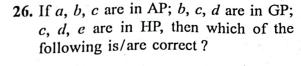
25. If a, b, c are the sides of triangle ABC, then what is



$$\begin{vmatrix} a^2 & b \sin A & c \sin A \\ b \sin A & 1 & \cos A \\ c \sin A & \cos A & 1 \end{vmatrix}$$
 equal to?

- 1 Zero
- (b) Area of triangle
- (c) Perimeter of triangle

$$-(d)$$
  $a^2+b^2+c^2$ 



1. a, c and e are in GP

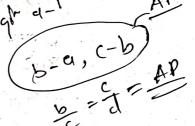
 $\chi$  2.  $\frac{1}{a}$ ,  $\frac{1}{c}$ ,  $\frac{1}{a}$  are in GP

Select the correct answer using the code given below:

(a) 1 only

Both 1 and 2

(d) Neither 1 nor 2



27. What is the number of solutions of  $log_4(x-1) = log_2(x-3)$ ?

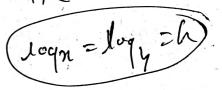
5 C(a) Zero

(d) Three Jog (2-1) - tog (2-

**28.** For  $x \ge y > 1$ ,

let  $log_x\left(\frac{x}{y}\right) + log_y\left(\frac{y}{x}\right) = k$ ,  $\frac{(x-1)(x-1)}{x-1-1-1}$ 

then the value of k can never be equal  $\lambda$ 



A - RRAN-B-MTH

29. If 
$$A = \begin{bmatrix} \sin 2\theta & 2\sin^2 \theta - 1 & 0 \\ \cos 2\theta & 2\sin \theta \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
, then

which of the following statements is/are correct?

$$1. A^{-1} = adjA$$

2. A is skew-symmetric matrix

3. 
$$A^{-1} = A^T$$

Select the correct answer using the code given below:

- (a) 1 only
- (b) 1 and 2

- (d) 2 and 3
- 30. What is the coefficient of  $x^{10}$  in the expansion of  $\left(1-x^2\right)^{20} \left(2-x^2-\frac{1}{x^2}\right)^{-5}$ ?

(a) 
$$-1$$

- (b) 1
- (c) 10
- (d) Coefficient of  $x^{10}$  does not exist

- 31. If the 4th term in the expansion of  $\left(mx + \frac{1}{x}\right)^n \text{ is } \frac{5}{2}, \text{ then what is the value of } mn?$ 
  - (a) -3
  - (3) 3
    - (c) 6
  - (d) 12
- 32. If a, b and c (a > 0, c > 0) are in GP, then consider the following in respect of the equation  $ax^2 + bx + c = 0$ :
  - 1. The equation has imaginary roots.

## 5 B Crack

- 2. The ratio of the roots of the equation is  $1:\omega$  where  $\omega$  is a cube root of unity.
- 3. The product of roots of the equation is  $\left(\frac{b^2}{a^2}\right)$ .

Which of the statements given above are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (a) 1, 2 and 3

- 33. If  $x^2 + mx + n$  is an integer for all integral values of x, then which of the following is/are correct?
  - 1. m must be an integer
  - 2. n must be an integer

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- Neither 1 nor 2
- 34. In a binomial expansion of  $(x+y)^{2n+1}(x-y)^{2n+1}$ , the sum of middle terms is zero. What

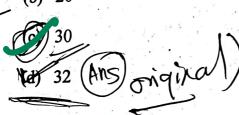
is the value of  $\left(\frac{x^2}{y^2}\right)$ ?



- (b) 2
- (c) 4
- (d) 8
- 35. Let  $A = \{1, 2, 3, 4, 5\}$  and  $B = \{6, 7\}$ . What is the number of onto functions from A to B?

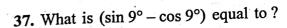


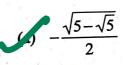
(b) 20



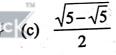
36. What is 
$$\frac{\sqrt{3}\cos 10^{\circ} - \sin 10^{\circ}}{\sin 25^{\circ}\cos 25^{\circ}}$$
 equal to ?

- (a) 1
- (b)  $\sqrt{3}$
- (c) 2
- (2) 4





(b)  $-\frac{\sqrt{5-\sqrt{3}}}{2}$ 



 $(d) \frac{\sqrt{5-\sqrt{5}}}{4}$ 



13 ccs 10 - simu

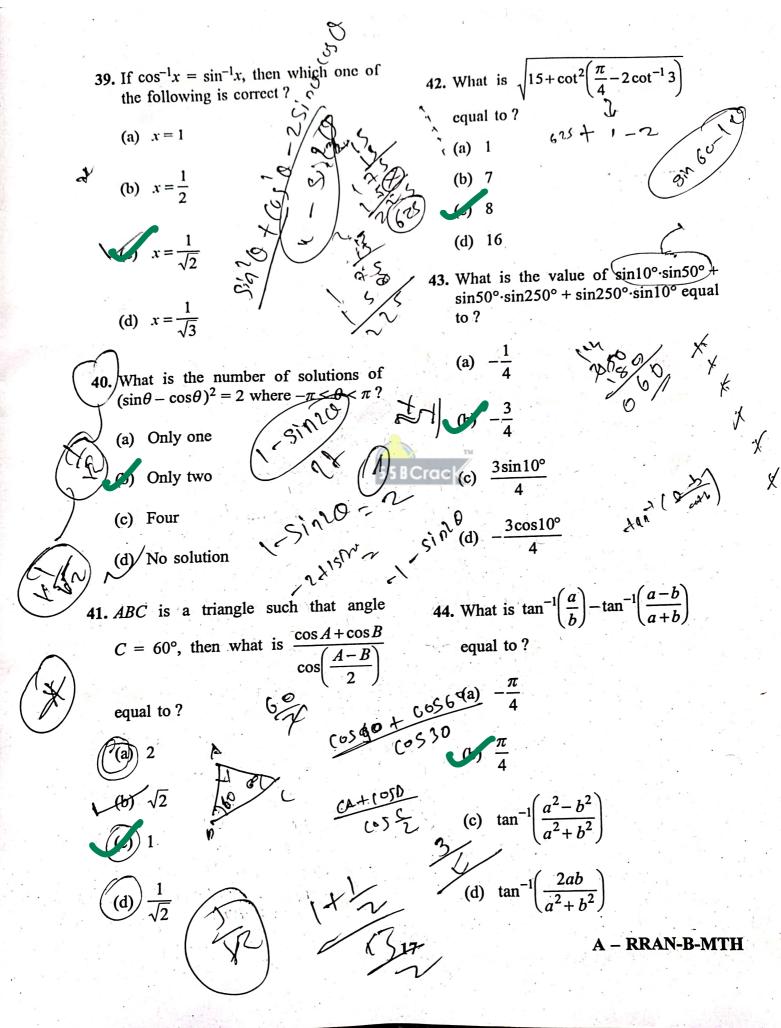
38. If in a triangle ABC,  $\sin^3 A + \sin^3 B + \sin^3 C = 3\sin A \sin B \sin C$ , then what is

the value of the determinant  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$ ;

where a, b, c are sides of the triangle?

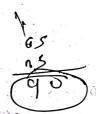
- (a) a + b + c
- (b) ab + bc + ca
- (c) (a+b)(b+c)(c+a)
- (d) 0

15



- 45. Under which one of the following conditions does the equation  $(\cos \beta 1)x^2 + (\cos \beta)x + \sin \beta = 0$  in x have a real root for  $\beta \in [0, \pi]$ ?
  - (a)  $1 \cos \beta < 0$
  - (b)  $1 \cos \beta \leq 0$
  - $(\beta) 1 \cos \beta > 0$ 
    - (d)  $1 \cos \beta \ge 0$
- 46. In a triangle ABC, AB = 16 cm, BC = 63 cm and AC = 65 cm. What is the value of  $\cos 2A + \cos 2B + \cos 2C$ ?

- 48. If  $\tan \alpha$  and  $\tan \beta$  are the roots of the equation  $x^2 6x + 8 = 0$ , then what is the value of  $\cos(2\alpha + 2\beta)$ ?
  - (a)  $\frac{13}{75}$
  - (b)  $\frac{13}{85}$
  - (c)  $\frac{17}{85}$
  - (d)  $\frac{19}{85}$



49. What is the value of  $\tan 65^{\circ} + 2\tan 45^{\circ} - 2\tan 40^{\circ} - \tan 25^{\circ}$ ?

- (2) -1
- (b) 0
- (c) 1
- (d)  $\frac{76}{65}$
- 47. If  $f(\theta) = \frac{1}{1 + \tan \theta}$  and  $\alpha + \beta = \frac{5\pi}{4}$ ,
  - then what is the value of  $f(\alpha) f(\beta)$ ?
  - (a)  $-\frac{1}{2}$
  - (b)  $\frac{1}{2}$
  - 14(e) 1
    - (d) 2 = 1+4an (T)

- 5 B Crac (a) 0 1 (b) 1 2 (c) 2 (c)
  - (d) 4

- Cos = OP
- 1. In a triangle ABC, if  $\cot A \cdot \cot B \cdot \cot C > 0$ , then the triangle is an acute angled triangle.

150. Consider the following statements:

2. In a triangle ABC, if  $\tan A \cdot \tan B \cdot \tan C > 0$ , then the triangle is an obtuse angled triangle.

Which of the statements given above is/are correct?

- (2) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2



- 51. If (a, b) is the centre and c is the radius of the circle  $x^2 + y^2 + 2x + 6y + 1 = 0$ , then what is the value of  $a^2 + b^2 + c^2$ ?
  - (·) 19
  - (b) 18
  - (c) 17
  - (d) 11
- 52. If (1, -1, 2) and (2, 1, -1) are the end points of a diameter of a sphere  $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz 1 = 0$ , then what is u + v + w equal to?
  - (a) -2
  - (b) -1
  - (c) 1
  - (°) 2
- 53. The number of points represented by the equation x = 5 on the xy-plane is
  - (a) Zero
  - (b) One
  - (c) Two
  - (d) Infinitely many

- 54. If < l, m, n > are the direction cosines of a normal to the plane 2x 3y + 6z + 4 = 0, then what is the value of  $49(7l^2 + m^2 n^2)$ ?
  - (a) 0
  - 0) 1
  - (c) 3
  - (d) 71
- 55. A line through (1, -1, 2) with direction ratios < 3, 2, 2 > meets the plane x + 2y + 3z = 18. What is the point of intersection of line and plane?

55BCracl

- (a) (4, 4, 1)
- (b) (2, 4, 1)
- (4, 1, 4)
- (d) (3, 4, 7)
- 56. If p is the perpendicular distance from origin to the plane passing through (1, 0, 0), (0, 1, 0) and (0, 0, 1), then what is  $3p^2$  equal to?
  - (a) 4
  - (b) 3
  - (c) 2
  - (d) 1

57. If the direction cosines < l, m, n > of a line are connected by relation l + 2m + n = 0, 2l - 2m + 3n = 0, then what is the value of  $l^2 + m^2 - n^2$ ?

(a) 
$$\frac{1}{101}$$

(3) 
$$\frac{29}{101}$$

(c) 
$$\frac{41}{101}$$

(d) 
$$\frac{92}{101}$$

58. If a variable line passes through the point of intersection of the lines x + 2y - 1 = 0 and 2x - y - 1 = 0 and meets the coordinate axes in A and B, then what is the locus of the mid-point of AB?

$$(a) 3x + y = 10xy$$

$$(b) x + 3y = 10xy$$

(c) 
$$3x + y = 10$$

(d) 
$$x + 3y = 10$$

59. What is the equation to the straight line passing through the point  $(-\sin\theta, \cos\theta)$  and perpendicular to the line  $x\cos\theta + y\sin\theta = 9$ ?

$$(s) x\sin\theta - y\cos\theta - 1 = 0$$

(b) 
$$x\sin\theta - y\cos\theta + 1 = 0$$

(c) 
$$x\sin\theta - y\cos\theta = 0$$

(d) 
$$x\cos\theta - y\sin\theta + 1 = 0$$

60. Two points P and Q lie on line y = 2x + 3. These two points P and Q are at a distance 2 units from another point R(1, 5). What are the coordinates of the points P and Q?

(a) 
$$\left(1+\frac{2}{\sqrt{5}}, 5+\frac{4}{\sqrt{5}}\right), \left(1-\frac{2}{\sqrt{5}}, 5-\frac{4}{\sqrt{5}}\right)$$

(b) 
$$\left(3+\frac{2}{\sqrt{5}}, 5+\frac{4}{\sqrt{5}}\right), \left(-1-\frac{2}{\sqrt{5}}, 5-\frac{4}{\sqrt{5}}\right)$$

(c)  $\left(1-\frac{2}{\sqrt{5}}, 5+\frac{4}{\sqrt{5}}\right), \left(1+\frac{2}{\sqrt{5}}, 5-\frac{4}{\sqrt{5}}\right)$ 

(d) 
$$\left(3 - \frac{2}{\sqrt{5}}, 5 + \frac{4}{\sqrt{5}}\right), \left(-1 + \frac{2}{\sqrt{5}}, 5 - \frac{4}{\sqrt{5}}\right)$$

- 61. If two sides of a square lie on the lines 2x+y-3=0 and 4x+2y+5=0, then what is the area of the square in square units?
  - (a) 6.05
  - (b) 6·15
  - 6.25
  - (d) 6.35

- 62. ABC is a triangle with A(3, 5). The mid-points of sides AB, AC are at (-1, 2), (6, 4) respectively. What are the coordinates of centroid of the triangle ABC?
  - (a)  $\left(\frac{8}{3}, \frac{11}{3}\right)$
- (a)  $\left(\frac{7}{3}, \frac{7}{3}\right)$ 
  - (c)  $(2, \frac{8}{3})$
  - (d)  $\left(\frac{8}{3}, 2\right)$
- 63. ABC is an acute angled isosceles triangle. Two equal sides AB and AC lie on the lines 7x-y-3=0 and x+y-5=0. If  $\theta$  is one of the equal 55 B Crack)  $\frac{1}{2}$ angles, then what is  $\cot \theta$  equal to?
  - (a)  $\frac{1}{3}$
- **64.** In the parabola  $y^2 = 8x$ , the focal distance of a point P lying on it is 8 units. Which of the following statements is/are correct?
  - 1. The coordinates of P can be  $(6, 4\sqrt{3}).$
  - 2. The perpendicular distance of Pfrom the directrix of parabola is 8 units.

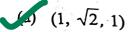
Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- Both 1 and 2
  - (d) Neither 1 nor 2
- 65. What is the eccentricity of the ellipse if the angle between the straight lines joining the foci to an extremity of the minor axis is 90°?
  - (a)  $\frac{1}{3}$

**66.** Let  $\vec{a} = \hat{i} - \hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ . If  $\overrightarrow{a} \times (\overrightarrow{b} \times \overrightarrow{a}) = \alpha \hat{i} - \beta \hat{j} + \gamma \hat{k}$ , then what 0x(bxci) =(axb) is the value of  $\alpha + \beta + \gamma$ ?

(d) 1

67. If a vector of magnitude 2 units makes an angle  $\frac{\pi}{3}$  with  $2\hat{i}$ ,  $\frac{\pi}{4}$  with  $3\hat{j}$  and an acute angle  $\theta$  with  $4\hat{k}$ , then what are the components of the vector?



(b) 
$$(1, -\sqrt{2}, 1)$$

(c) 
$$(1, -\sqrt{2}, -1)$$

(d) 
$$(1, \sqrt{2}, -1)$$

- 68. Consider the following in respect of moment of a force:
  - 1. The moment of force about a point is independent of point of application of force.
  - 2. The moment of a force about a line is a vector quantity.

Which of the statements given above is/are correct?

- (a) 1 only
- (b) 2 only
- Both 1 and 2
- (d) Neither 1 nor 2
- 69. For any vector  $\vec{r}$ , what is  $(\vec{r} \cdot \hat{i})(\vec{r} \times \hat{i}) + (\vec{r} \cdot \hat{j})(\vec{r} \times \hat{j}) + (\vec{r} \cdot \hat{k})(\vec{r} \times \hat{k})$ equal to  $\hat{i}$



- (b)  $\overline{r}$
- (c)  $2\vec{r}$
- (d)  $3\vec{r}$



- 70. Let  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two vectors of magnitude 4 inclined at an angle  $\frac{\pi}{3}$ , then what is the angle between  $\overrightarrow{a}$  and  $\overrightarrow{a} \overrightarrow{b}$ ?
  - (a)  $\frac{\pi}{2}$
- 1
- (b)  $\frac{it}{3}$ 
  - (c)  $\frac{\pi}{4}$
  - (d)  $\frac{\pi}{6}$



71. Let  $y_1(x)$  and  $y_2(x)$  be two solutions of the differential equation  $\frac{dy}{dx} = x$ . If

 $y_1(0) = 0$  and  $y_2(0) = 4$ , then what is the number of points of intersection of the curves  $y_1(x)$  and  $y_2(x)$ ?

- (a) No point
  - (b) One point
  - (c) Two points
  - (d) More than two points
- 72. The differential equation, representing the curve  $y = e^x(a \cos x + b \sin x)$  where a and b are arbitrary constants, is

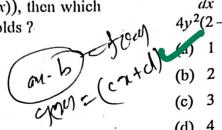
$$(a) \quad \frac{d^2y}{dx^2} + 2y = 0$$

(b) 
$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + 2y = 0$$

(c) 
$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 2y = 0$$

$$(d) \frac{d^2y}{dx^2} + y = 0$$

73. If f(x) = ax - b and g(x) = cx + d are such that f(g(x)) = g(f(x)), then which one of the following holds?



$$(a) f(d) = g(b)$$

$$(b) f(b) + g(d) = 0$$

(c) 
$$f(a) + g(c) = 2a$$
  
 $f(d) + g(b) = 2d$ 

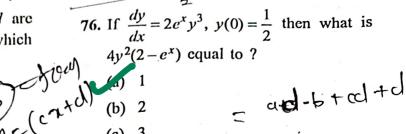
- 74. What is  $\int_{-1}^{1} (3\sin x \sin 3x) \cos^2 x dx$ equal to?



- (d)
- 75. What are the order and degree respectively of the differential equation

$$\left\{2 - \left(\frac{dy}{dx}\right)^2\right\}^{0.6} = \frac{d^2y}{dx^2} ?$$

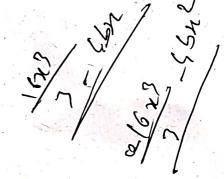
- (a) 2, 2
- (b) 2, 3
- (4) 2, 5



- (d) 4
- 77. Let  $p = \int_a^b f(x)dx$  and  $q = \int_a^b |f(x)|dx$ . If  $f(x) = e^{-x}$ , then which one of the following is correct?
  - (a) p = 2q
- 78. What is  $\int_0^{\frac{\pi}{2}} \frac{a + \sin x}{2a + \sin x + \cos x} dx$  equal



- (b)  $\frac{\pi}{2}$
- (c) 1
- (d) 0



- The non-negative values of b for which the function  $\frac{16x^3}{3} - 4bx^2 + x$  has neither maximum nor minimum in the range x > 0 is
  - (a) 0 < b < 1
  - (b) 1 < b < 2
  - (c) b > 2
  - (d)  $0 \le b < 1$

80. Which one of the following is correct in respect of  $f(x) = \frac{1}{\sqrt{|x| - x}}$  and

$$g(x) = \frac{1}{\sqrt{x - |x|}}$$
?

f(x) has some domain and g(x) has no domain

- (b) f(x) has no domain and g(x) has some domain
- (c) f(x) and g(x) have the same domain
- (d) f(x) and g(x) do not have any domain

Consider the following for the next two (02) items that follow:

Given that  $\int \frac{3\cos x + 4\sin x}{2\cos x + 5\sin x} dx =$  $\frac{\alpha x}{29} + \frac{\beta}{29} \ln \left| 2\cos x + 5\sin x \right| + c$ 

- 81. What is the value of  $\alpha$ ?
  - (a) 7.
  - 13
  - (c) 17
- 82. What is the value of  $\beta$ ?

- (b) 13
- (c) 1:7
- (d) 26

Consider the following for the next two (02) items that follow:

Let 
$$f(x) = \frac{x}{\ln x}$$
;  $(x > 1)$ 

83. Consider the following statements:

1./f(x) is increasing in the interval  $(e, \infty)$ 

2.f(x) is decreasing in the interval 7 not onders to 3. 9ln7 > 7ln9

Which of the statements given above are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- te f"=0
- (2) 1, 2 and 3

55 BCrac(c) 1 and 3 only

- 84. Consider the following statements:
  - 1.  $f''(e) = \frac{1}{e}$
  - 2. f(x) attains local minimum value
  - 3. A local minimum value of f(x)- is e

Which of the statements given above are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

Let f(x) and g(x) be two functions such that

$$g(x) = x - \frac{1}{x}$$
 and  $f \circ g(x) = x^3 - \frac{1}{x^3}$ .

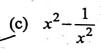
85. What is g[f(x) - 3x] equal to?

Which of the statements given above are correct?

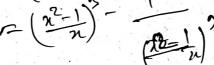
- 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

 $(x)^3 - \frac{1}{x^3}$ 





(d) 
$$x^2 + \frac{1}{x^2}$$





86. What is f''(x) equal to?

(a) 
$$-\frac{2}{x^3}$$

(b) 
$$2x + \frac{2}{x^3}$$

(c) 
$$6x + 3$$

$$(d)$$
  $6x$ 

Consider the following for the next two (02) items that follow:

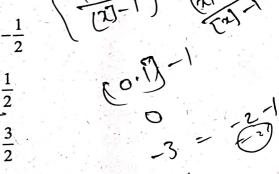
Let f(x) = |x| + 1 and g(x) = [x] - 1, where [.] is the greatest integer function.

Let 
$$h(x) = \frac{f(x)}{g(x)}$$

87. Consider the following statements:

- 1. f(x) is differentiable for all x < 0
- 2. g(x) is continuous at x = 0.0001
- 3. The derivative of g(x) at x = 2.5 is 1

88. What is  $\lim_{x\to 0^-} h(x) + \lim_{x\to 0^+} h(x)$  equal  $\lim_{x\to 0^+} h(x) = \lim_{x\to 0^+} h(x)$  equal  $\lim_{x\to 0^+} h(x) = \lim_{x\to 0^+} h(x) = \lim_{x$ 



Consider the following for the next two (02) items that follow:

Let 
$$\varphi(a) = \int_{a}^{a+100\pi} |\sin x| dx$$

89. What is  $\varphi(a)$  equal to?

- (a) 0
- (b) a
- (c) 100a
- (2) 200

90. What is  $\varphi'(a)$  equal to?

- 6,0
- (b) π
- (c) 100
- (d) 200

Consider the following for the next two (02)

A differentiable function f(x) has a local maximum at x = 0. Let y = 2f(x) + ax - b.

- 91. Which of the following is/are correct?
  - 1. f'(0) = 0
  - 2. f''(0) < 0

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
  - Both 1 and 2
  - (d) Neither 1 nor 2
- 92. The function y has a relative maxima at x = 0 for
  - (a) a > 0, b = 0
  - for all b and a=0
  - (c) for all b > 0 only
  - (d) for all a and b = 0

Consider the following for the next two (02) items that follow:

Let f(x) = |x - 1|, g(x) = [x] and h(x) = f(x)g(x) where [.] is greatest integer function.

- 93. What is  $\int_{-1}^{0} h(x)dx$  equal to?
  - (a)  $-\frac{3}{2}$
  - (b) -1

- (c) 0
- (d)  $\frac{1}{2}$
- 94. What is  $\int_0^2 h(x)dx$  equal to?
  - (a)  $-\frac{3}{2}$ 
    - (b) -1
    - (c) 0
  - (d)  $\frac{1}{2}$

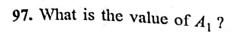
Consider the following for the next two (02) items that follow:

Let 
$$\int \frac{dx}{\sqrt{x+1} - \sqrt{x-1}} = \alpha(x+1)^{\frac{3}{2}} + \beta(x-1)^{\frac{3}{2}} + c$$

55BCrack

- 95. What is the value of  $\alpha$ ?
  - (a)  $\frac{1}{3}$
  - (b)  $\frac{2}{3}$
  - (c) 1
  - (d)  $\frac{4}{3}$
- 96. What is the value of  $\beta$ ?
  - (a)  $-\frac{2}{3}$
  - (b)  $-\frac{1}{3}$
  - (c)  $\frac{1}{3}$
  - (d)  $\frac{2}{3}$

The circle  $x^2 + y^2 - 2x = 0$  is partitioned by line y = x in two segments. Let  $A_1$ ,  $A_2$  be the areas of major and minor segments respectively.

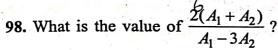


(a) 
$$\frac{\pi-2}{4}$$

(b) 
$$\frac{\pi+2}{4}$$







- (b) 1
- (c) -1
- (d)  $-\pi$

Consider the following for the next two (02) items that follow:

Let 
$$3f(x) + f\left(\frac{1}{x}\right) = \frac{1}{x} + 1$$

99. What is f(x) equal to?

(a) 
$$\frac{1}{8x} - \frac{x}{8} + \frac{1}{4}$$

(b) 
$$\frac{3}{8x} - \frac{x}{8} + \frac{3}{4}$$

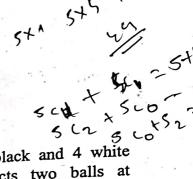
(c) 
$$\frac{3}{8x} + \frac{x}{8} + \frac{1}{4}$$

$$\frac{3}{8x} - \frac{x}{8} + \frac{1}{4}$$

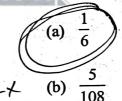
100. What is 
$$8\int_{1}^{2} f(x)dx$$
 equal to?



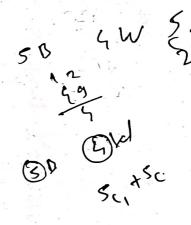
- ) (b)  $ln(4\sqrt{e})$ 
  - (c) ln 2
  - (d) ln 2 1



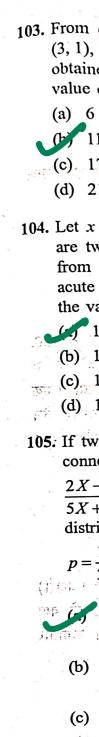
halls. A man selects two balls at random. What is the probability that both of these are of the same colour?



- (c)  $\frac{4}{9}$
- $\sqrt{(d)} \frac{5}{18}$



- 102. If a random variable (x) follows binomial distribution with mean 5 and variance 4, and  $5^{23}P(X=3) = \lambda 4^{\lambda}$ , then what is the value of  $\lambda$ ?
  - (a) 3
  - (b) 5
  - (c) 23
  - (d) 25



(d)

- 103. From data (-4, 1), (-1, 2), (2, 7) and (3, 1), the regression line of y on x is obtained as y = a + bx, then what is the value of 2a + 15b? (d) 21 104. Let x + 2y + 1 = 0 and 2x + 3y + 4 = 0are two lines of regression computed from some bivariate data. If  $\theta$  is the acute angle between them, then what is the value of 488tan30?
  - 105. If two random variables X and Y are connected by relation  $\frac{2X-3Y}{5X+4Y} = 4$  and X follows Binomial distribution with parameters n = 10 and  $p = \frac{1}{2}$ , then what is the variance of Y?

106. If a, b, c are in HP, then what is

2.  $\frac{1}{a} + \frac{1}{c}$ 3.  $\frac{1}{2} \left( \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right)$ 

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) 3 only
- (d) 1, 2 and 3
- 107. An edible oil is sold at the rates 150, 200, 250, 300 rupees per litre in four consecutive years. Assuming that an equal amount of money is spent on oil by a family in every year during these years, what is the average price of oil in rupees (approximately) per litre?
  - (a) 210 (b) 220
- 66 108. If the letters of the word "TIRUPATI" are written down at random, then what is the probability that both Ts are always consecutive?
- 60 900
- (c)

- RRAN-B-MTH

 $\frac{1}{b-a} + \frac{1}{b-c}$  equal to ?

- 109. Let  $m = 77^n$ . The index n is given a positive integral value at random. What is the probability that the value of m will have 1 in the units place?
  - (a)  $\frac{1}{2}$
  - (b)  $\frac{1}{3}$
  - $\frac{1}{4}$ 
    - (d)  $\frac{1}{n}$
- 110. Three different numbers are selected at random from the first 15 natural numbers. What is the probability that the product of two of the numbers is equal to third number?
  - (a)  $\frac{1}{91}$
  - (b)  $\frac{2}{455}$
  - (c)  $\frac{1}{65}$ 
    - (d)  $\frac{6}{455}$

Let A and B be two events such that  $P(A \cup B) \ge 0.75$  and  $0.125 \le P(A \cap B) \le 0.375$ .

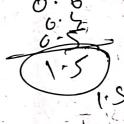
- 111. What is the minimum value of P(A) + P(B)?
  - (a) 0.625
  - (b) 0.750
  - (c) 0.825
  - (d) 0.875
- 112. What is the maximum value of P(A) + P(B)?
  - (a) 0.75
  - 1.125
    - (c) 1·375
    - (d) 1.625

Consider the following for the next two (02) items that follow:

A, B and C are three events such that P(A) = 0.6, P(B) = 0.4, P(C) = 0.5,  $P(A \cup B) = 0.8$ ,  $P(A \cap C) = 0.3$  and  $P(A \cap B \cap C) = 0.2$  and

P(AUBUC) ≥ 0.85. P(A)+P(D)+P()-P(UD)-P(DUC) r(AVC)+5

- 113. What is the minimum value of  $P(B \cap C)$ ?
  - (a) 0·1
  - 00) 0.2
  - (c) 0·35
  - (d) 0.45



- 114. What is the maximum value of  $P(B \cap C)$ ?
  - (a) 0·1
  - (b) 0·2
  - 0.35
  - (d) 0·45

An unbiased coin is tossed n times. The probability of getting at least one tail is p and the probability of at least two tails is q and  $p-q=\frac{5}{32}$ .

- 115. What is the value of n?
  - (a) 4
  - (b) 5
  - (c) 6
  - C3 7
- 116. What is the value of p+q?

$$\frac{57}{32}$$

(b) 
$$\frac{53}{32}$$

(c) 
$$\frac{51}{32}$$
 (d) 1

Consider the following for the next two (02) items that follow:

$x_i$	1	2	3	•••	n
$f_i$	1	2-1	2-2	•	$2^{-(n-1)}$

117. What is  $\sum_{i=1}^{n} x_i f_i$  equal to?

$$(4a)^{n+1} \frac{2^{n+1} - n + 2}{2^{n-1}}$$

$$\frac{2^{n+1}-n-2}{2^{n-1}}$$

(c) 
$$\frac{2^{n+1}+n+2}{2^{n-1}}$$

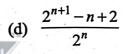
(d) 
$$\frac{2^{n+1}-n-2}{2^n}$$

118. What is the mean of the distribution?

(a) 
$$\frac{2^{n+1}-n+2}{2^n-1}$$

(b) 
$$\frac{2^{n+1}-n-2}{2^{n-1}}$$

(c) 
$$\frac{2^{n+1}-n-2}{2^n-1}$$





Consider the following for the next two (02) items that follow:

The marks obtained by 10 students in a Statistics test are 24, 47, 18, 32, 19, 15, 21, 35, 50 and 41

119. What is the mean deviation of the largest five observations?

- (b) 5·5
- (c) 6
- (d) 7.5
- 120. What is the variance of the largest five observations?
  - (a) 14·6
  - (b) 21·8
  - (c) 25·2
  - (2) 46.8