

# NDA 1 2025

LIVE

# MATHS

## SETS-RELATION FUNCTION

CLASS 2

NAVJYOTI SIR

Crack  
EXAMS



## 04 Oct 2024 Live Classes Schedule

9:00AM --- 04 OCTOBER 2024 DAILY DEFENCE UPDATES --- DIVYANSHU SIR

### SSB INTERVIEW LIVE CLASSES

9:00AM --- OVERVIEW ON OIR & PRACTICE --- ANURADHA MA'AM

### NDA 1 2025 LIVE CLASSES

1:00PM --- BIOLOGY - ANIMAL KINGDOM --- SHIVANGI MA'AM

4:00PM --- MATHS - SETS, RELATION & FUNCTION - CLASS 2 --- NAVJYOTI SIR

5:30PM --- ENGLISH - SPOTTING ERRORS - CLASS 2 --- ANURADHA MA'AM

### CDS 1 2025 LIVE CLASSES

1:00PM --- BIOLOGY - ANIMAL KINGDOM --- SHIVANGI MA'AM

2:30PM --- MATHS - SI & CI - CLASS 3 --- NAVJYOTI SIR

5:30PM --- ENGLISH - SPOTTING ERRORS - CLASS 2 --- ANURADHA MA'AM

### AFCAT 1 2025 LIVE CLASSES

2:30PM --- MATHS - SI & CI - CLASS 3 --- NAVJYOTI SIR

4:00PM --- STATIC GK - SPORTS & GAMES TERMINOLOGY - 2 --- DIVYANSHU SIR

5:30PM --- ENGLISH - SPOTTING ERRORS - CLASS 2 --- ANURADHA MA'AM



# LAW OF ALGEBRA OF SETS

## 1. Idempotent laws

(a)  $A \cup A = A$

(b)  $A \cap A = A$

## 2. Identity laws

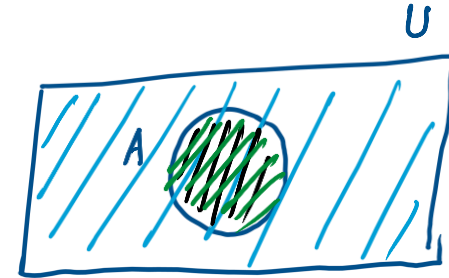
(a)  $A \cup \phi = A$  ✓

(b)  $A \cap U = A$  ✓

## 3. Commutative laws

(a)  $A \cup B = B \cup A$  ✓

(b)  $A \cap B = B \cap A$  ✓



# LAW OF ALGEBRA OF SETS

## 5. Distributive laws

$$(a) A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

$$(b) A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

## 6. De-Morgan's laws

$$\# (a) (A \cup B)' = A' \cap B' \quad (b) (A \cap B)' = A' \cup B'$$

$$(A \cup B)' = A' \cap B'$$

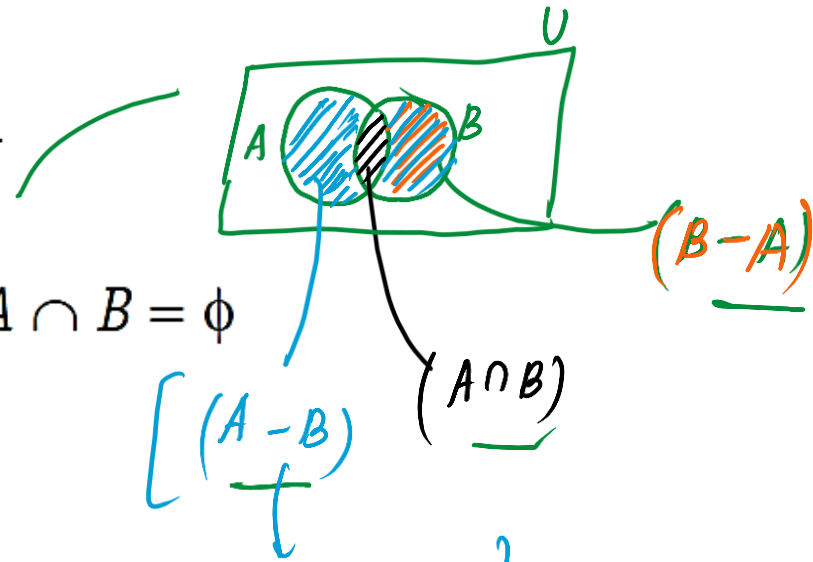
$$a \times (b+c) = \underline{a \times b + a \times c}$$



# IMPORTANT RESULTS

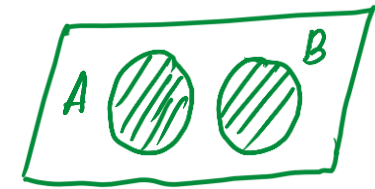
If  $A$ ,  $B$  and  $C$  are any three finite sets, then

1.  $n(A \cup B) = n(\underline{A}) + n(\underline{B}) - n(\underline{A \cap B})$  ✓
2.  $n(A \cup B) = n(A) + n(B)$ , if and only if  $A \cap B = \phi$
3.  $n(A - B) = n(A) - n(A \cap B)$



$$n(A \cup B) = n(A) + n(B) - n(\underline{A \cap B}) = \underline{A - A \cap B}$$

If  $A \cap B = \phi$  ( $A$  &  $B$  are disjoint sets)  $n(A \cap B) = 0$



$$n(A \cup B) = n(A) + n(B)$$

$$n(\underline{A - B}) = \underline{n(A) - n(A \cap B)}$$

# IMPORTANT RESULTS

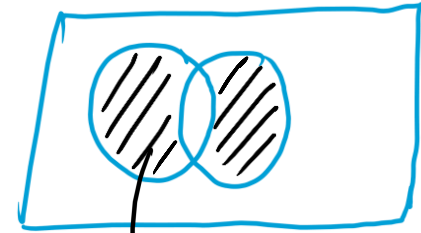
4.  $n(A \Delta B) = n(A - B) + n(B - A) = n(A) + n(B) - 2n(A \cap B)$

5.  $n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(A \cap C) + n(A \cap B \cap C)$

6.  $n(A' \cup B') = n(U) - n(A \cap B)$

7.  $n(A' \cap B') = n(U) - n(A \cup B)$

4.)  $n(A \Delta B) = n(A - B) + n(B - A) = n(A) + n(B) - 2n(A \cap B)$

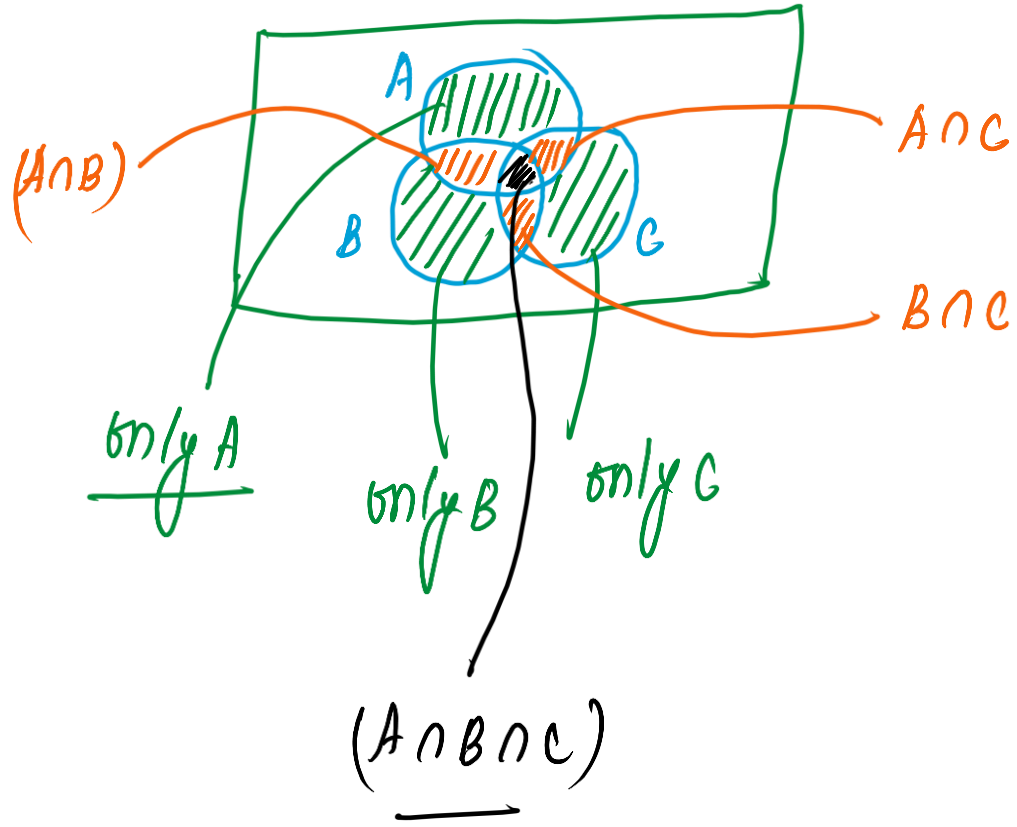


$(A - B) \cup (B - A)$

$[A - (A \cap B)] \cup [B - (B \cap A)]$



$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(C \cap A) + n(A \cap B \cap C)$$



$$\underline{n(A \cup B \cup C \cup D)} = ?$$

$$6.) \quad n(A' \cap B') = n(\underline{A \cup B})'$$

$$A' \cap B' = \underline{(A \cup B)'}$$

(For any set A,  $A' = U - A$ )  $\rightarrow$   $n(A') = n(U) - n(A)$

$$= n(U) - \underline{n(A \cup B)}$$

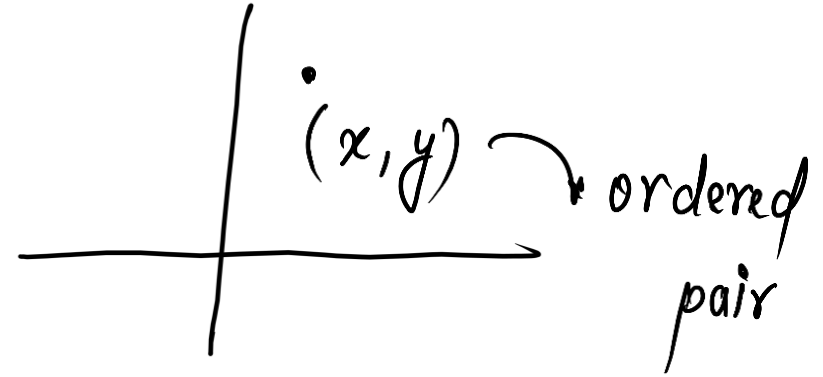
$$7.) \quad n(A' \cup B') = n(A \cap B)' = n(U) - n(A \cap B)$$



# CARTESIAN PRODUCT

$$A = \{1, 2, 3\}$$

$$B = \{a, b\}$$



$$A \times B = \{(\underline{1}, \check{a}), (\underline{1}, \check{b}), (\check{2}, a), (\check{2}, b), (\check{3}, a), (\check{3}, b)\}$$

$$B \times A = \{(\underline{a}, 1), (\underline{b}, 1), (a, 2), (b, 2), (a, 3), (b, 3)\}$$

Cartesian product is set of ordered pairs,

→  $A \times B \neq B \times A$  (not commutative)

→  $(x+2, y+3) = (1, 3)$

$\Rightarrow x+2=1 \quad y+3=3$

$x = -1$

$y = 0$

$A = \{1, 2, 3\}$        $A = \{1, 2, 3\}$

$A \times A = \{(1,1), (1,2), (1,3), (2,1), (2,2), (2,3), (3,1), (3,2), (3,3)\}$

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$$* A \times B \times C = \{ (a, b, c) : a \in A, b \in B \text{ and } c \in C \}$$

↑  
ordered triple

$$* \text{If } n(A) = m \quad ; \quad n(B) = n$$

$$n(\underline{A \times B}) = \underline{m \times n}$$

# RELATION

$$A = \{1, 2, 3\} \quad B = \{a, b\}$$

$$A \times B = \{ \underline{(1, a)}, \underline{(1, b)}, \underline{(2, a)}, \underline{(2, b)}, (3, a), (3, b) \}$$

$$R \subseteq A \times B$$

(Any subset of  $A \times B$  (cartesian product) is a relation from  
A to B.

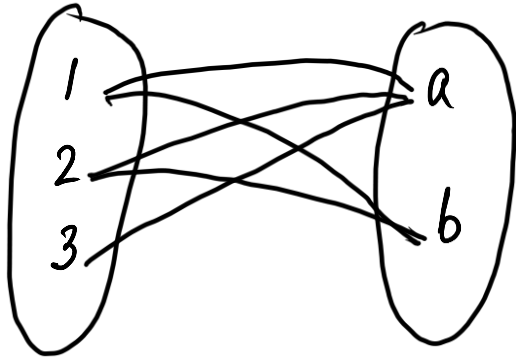
Eg :  $R_1 = \{(1, a), (2, b)\}$        $R_3 = \{\} = \emptyset$

$R_2 = \{(2, a), (3, a), (3, b)\}$        $R_4 = \underline{A \times B}$

# RELATION

$$R = \{(1, a), (1, b), (2, a), (2, b), (3, a)\}$$


 $R$  is a relation from  $A$  to  $B$ .



$R$  is a relation in  $N$ ; where,  $R = \{(a, b) : a > b, a, b \in N\}$

$$R = \{(2, 1), (3, 2), (3, 1), \dots\}$$

# DOMAIN AND RANGE

$$R = \{(\underline{1}, \underline{a}), (\underline{2}, \underline{b}), (\underline{3}, \underline{c})\}$$

(R from A to B)

$$\left| \begin{array}{l} \underline{A} = \{1, 2, 3\} \\ B = \{a, b, c\} \end{array} \right.$$

$\{1, 2, 3\} \rightarrow$  Domain — set of first elements of the ordered pairs in R.

$\{a, b, c\} \rightarrow$  Range — set of second elements of the ordered pairs in R.



# TYPES OF RELATION

① Empty relation :  $\emptyset = \{ \}$

② Universal relation :  $A \times B =$  The whole cartesian product.

③ Identity relation :

$$R = \{ (1, 1), (2, 2), (3, 3) \dots \}$$

first element = second element.

# TYPES OF RELATION

**Inverse relation** If  $R$  is a relation on  $A$ , then the relation  $R^{-1}$  on  $A$ , defined by  $R^{-1} = \{(b, a) : (a, b) \in R\}$  is called an inverse relation to  $A$ .

Clearly,  $\text{domain}(R^{-1}) = \text{range}(R)$

and  $\text{range}(R^{-1}) = \text{domain}(R)$



$$R = \{ \underline{(1, a)}, (2, b) \}$$

$$R^{-1} = \{ (a, 1), \underline{(b, 2)} \}$$

# TYPES OF RELATION

① Reflexive Relation :

$$A = \{1, 2, 3\}$$

$$R_1 \text{ on } A = \{(1, 1), (2, 2), (3, 3)\}$$

$$R_2 = \{(1, 1), (2, 3)\}$$

if  $a \in A \Rightarrow \underline{(a, a) \in R}$

$R_1$  is reflexive ;  $R_2$  is not reflexive.

② symmetric :

$$R_1 = \{(1, 1), (2, 3), (3, 2)\} \checkmark$$

$$R_2 = \{(1, 3), (1, 2), (2, 2), (3, 1), (3, 2)\}$$

if  $(a, b) \in R \forall a, b \in A$

$\Rightarrow \underline{(b, a) \in R}$

$R_1$  is symmetric ;  $R_2$  is not.

$$A = \{1, 2, 3, 4\}$$

Transitive :

$$R_1 = \{ \underline{(1, 2)}, \underline{(3, 3)}, \underline{(4, 3)}, \underline{(3, 2)}, \underline{(4, 2)}, \underline{(2, 2)} \}$$

if  $\underline{(a, b)}$  and  $\underline{(b, c)} \in R$ ,  
then  $\underline{(a, c)} \in R$

$R_1$  is transitive.

$$R_2 = \{ \underline{(1, 2)}, \underline{(3, 4)}, \underline{(1, 4)} \}$$

$\underline{(a, b)}$  ✓ present  $\rightarrow$  but  
correspondingly  $\underline{(b, c)} \notin R$ ,

$R_2$  is transitive

$$R_3 = \{ \underline{(1, 2)}, \underline{(2, 4)}, \underline{(1, 3)} \}$$

$\rightarrow R_3$  is not transitive,

# TYPES OF RELATION

(iii) **Transitive relations** A relation  $R$  on a set  $A$  is said to be a transitive relation, if  $(a, b) \in R$ ,  $(b, c) \in R \Rightarrow (a, c) \in R$ .

In other words, if  $a$  is related to  $b$ ,  $b$  is related to  $c$ , then  $a$  is related to  $c$ .

Transitivity fails only when there exists  $a, b$  and  $c$  such that  $aRb$ ,  $bRc$  but  $a \not R c$ .

e.g., let  $A = \{1, 2, 3\}$  and the relation

$$R = \{(1, 2), (2, 1), (1, 1)\}.$$

Then,  $R$  is not transitive, since  $R$ ,

$$(2, 1) \in R, (1, 2) \in R \text{ but } (2, 2) \notin R.$$

# TYPES OF RELATION

## EQUIVALENCE RELATION

A relation  $R$  on a set  $A$  is said to be an equivalence relation, if

- (i)  $R$  is reflexive *i.e.*,  $(a, a) \in R, \forall a \in A$  ✓
- (ii)  $R$  is symmetric *i.e.*,  $(a, b) \in R \Rightarrow (b, a) \in R, \forall a, b \in A$  ✓
- (iii)  $R$  is transitive *i.e.*,  $(a, b), (b, c) \in R \Rightarrow (a, c) \in R$  ✓

• Universal and Identity relation are equivalence relation.



Q) Which of the following statements is not correct for the relation  $R$  defined by  $aRb$  if and only if  $b$  lives within one kilometer from  $a$ ?

- (a)  $R$  is reflexive                      (b)  $R$  is symmetric  
(c)  $R$  is not anti-symmetric        (d) None of the above

Q) Which of the following statements is not correct for the relation  $R$  defined by  $aRb$  if and only if  $b$  lives within one kilometer from  $a$ ?

- (a)  $R$  is reflexive                      (b)  $R$  is symmetric  
(c)  $R$  is not anti-symmetric        (d) None of the above

Ans: (b)

Q) A relation  $R$  is defined on the set  $Z$  of integers as follows :

$$mRn \Leftrightarrow m + n \text{ is odd.}$$

Which of the following statements is/are true for  $R$  ?

1.  $R$  is reflexive
2.  $R$  is symmetric
3.  $R$  is transitive

Select the correct answer using the code given below :

- |             |             |
|-------------|-------------|
| (a) 2 only  | (b) 2 and 3 |
| (c) 1 and 2 | (d) 1 and 3 |

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Select the correct answer using the code given below :

- |             |             |
|-------------|-------------|
| (a) 2 only  | (b) 2 and 3 |
| (c) 1 and 2 | (d) 1 and 3 |

**Ans: (a)**

# Summary

- Cartesian Product
- Relations
- Types of Relations
- Practise Questions



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LIVE

# MATHS

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CLASS 3

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