

CDS 1 2025

MATHS

LIVE 

GEOMETRY

CLASS 2



NAVJYOTI SIR





6 Nov 2024 Live Classes Schedule

8:00AM -- 06 NOVEMBER 2024 DAILY CURRENT AFFAIRS RUBY MA'AM

9:00AM -- 06 NOVEMBER 2024 DAILY DEFENCE UPDATES DIVYANSHU SIR

SSB INTERVIEW LIVE CLASSES

9:30AM -- OVERVIEW OF OIR & PRACTICE ANURADHA MA'AM

NDA 1 2025 LIVE CLASSES

✓ 11:30AM -- GK - MEDIEVAL HISTORY - CLASS 2 RUBY MA'AM

✓ 1:00PM -- CHEMISTRY MCQ - CLASS 4 SHIVANGI MA'AM

✓ 4:00PM -- MATHS - PERMUTATION & COMBINATION - CLASS 1 NAVJYOTI SIR

✓ 6:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM

CDS 1 2025 LIVE CLASSES

✓ 11:30AM -- GK - MEDIEVAL HISTORY - CLASS 2 RUBY MA'AM

✓ 1:00PM -- CHEMISTRY MCQ - CLASS 4 SHIVANGI MA'AM

✓ 5:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM

✓ 7:00PM -- MATHS - GEOMETRY - CLASS 2 NAVJYOTI SIR

AFCAT 1 2025 LIVE CLASSES

✓ 4:00PM -- STATIC GK - COUNTRY CAPITAL CURRENCY - CLASS 2 DIVYANSHU SIR

✓ 5:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM



POLYGON

A plane figure formed by three or more non-collinear points joined by line segments is called a polygon.

A polygon with 3 sides is called a triangle.

A polygon with 4 sides is called a quadrilateral.

A polygon with 5 sides is called a pentagon.

A polygon with 6 sides is called a hexagon. ✓

A polygon with 7 sides is called a heptagon.

A polygon with 8 sides is called an octagon. ✓

A polygon with 9 sides is called a nonagon.

A polygon with 10 sides is called a decagon.

POLYGON

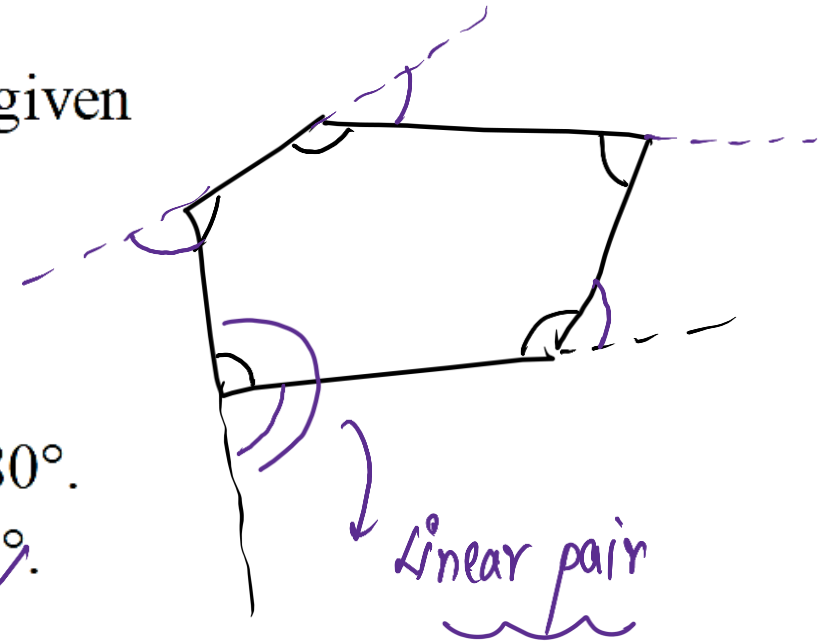
Regular polygon : A polygon in which all its sides and angles are equal, is called a regular polygon.

Sum of all interior angles of a regular polygon of side n is given by $(2n - 4) 90^\circ = (n - 2) \times 180^\circ$

Hence, angle of a regular polygon = $\frac{(2n - 4)90^\circ}{n}$

Sum of an interior angle and its adjacent exterior angle is 180° .

Sum of all exterior angles of a polygon taken in order is 360° .



$$\frac{360^\circ}{\text{number of sides}} = \text{measure of 1 exterior angle}$$

Q) The sum of the interior angles of a polygon is 1620° . The number of sides of the polygon are :

(a) 9

(b) 11

(c) 15

(d) 12

$$(n-2) \times 180^\circ = 1620^\circ$$

$$n-2 = \frac{1620^\circ}{180^\circ} = 9$$

$$n = 11$$

Q)The sum of the interior angles of a polygon is 1620° . The number of sides of the polygon are :

(a) 9

(b) 11

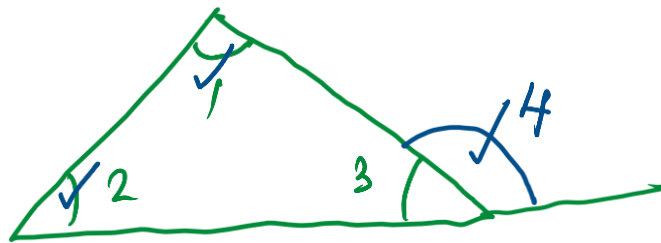
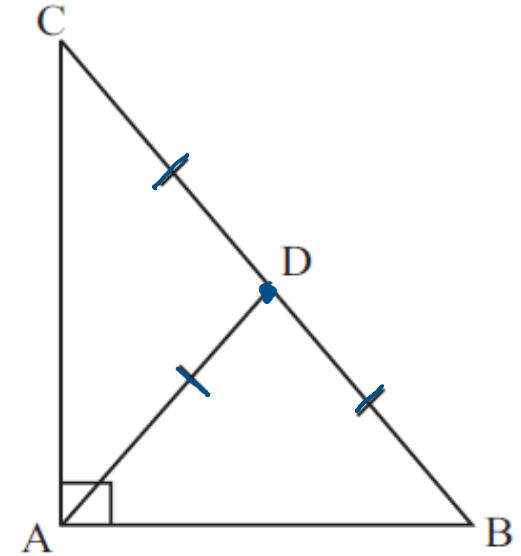
(c) 15

(d) 12

Ans: (b)

TRIANGLE IMPORTANT PROPERTIES

- The exterior angle of a triangle is equal to the sum of the opposite (not adjacent) interior angles ✓
- Sum of the lengths of any two sides of a triangle is greater than the length of the third side. (*difference less than third*)
- In any triangle, side opposite to greatest angle is largest and side opposite to smallest angle is smallest.
- In a right angled triangle, the line joining the vertex of the right angle to the mid point of the hypotenuse is half the length of the hypotenuse.



$$1 + 2 + 3 = 180^\circ$$

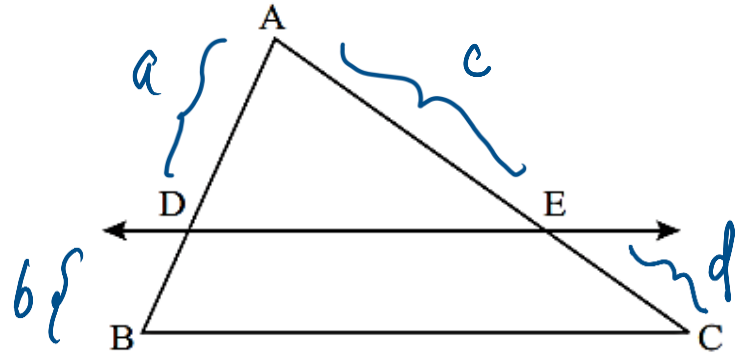
$$3 + 4 = 180^\circ$$

$$\underline{1 + 2 + 3 = 3 + 4} \Rightarrow$$

$$1 + 2 = 4$$

BASIC PROPORTIONALITY THEOREM

If a line is drawn parallel to one side of a triangle which intersects the other two sides in distinct points, the other two sides are divided in the same ratio.



$$\frac{a}{b} = \frac{c}{d} \checkmark$$

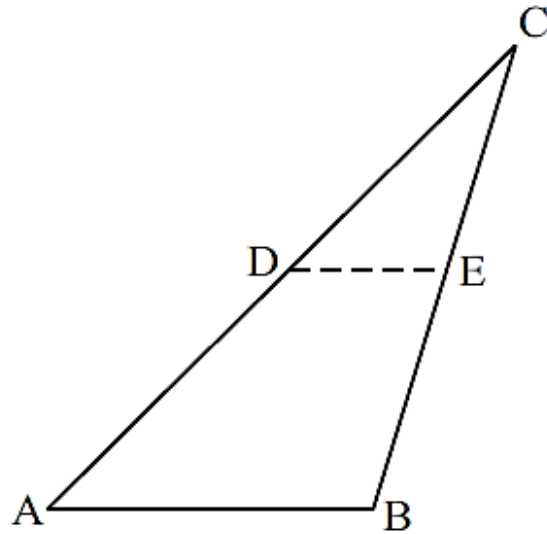
In $\triangle ABC$, $DE \parallel BC$,

Then, $\frac{AD}{DB} = \frac{AE}{EC}$

→ converse is true.

TRIANGLE IMPORTANT PROPERTIES

In any triangle, line segment joining the mid points of any two sides is parallel to the third side and equal to half of the length of third side.



In $\triangle ABC$, D and E are mid points of sides AC and BC , then

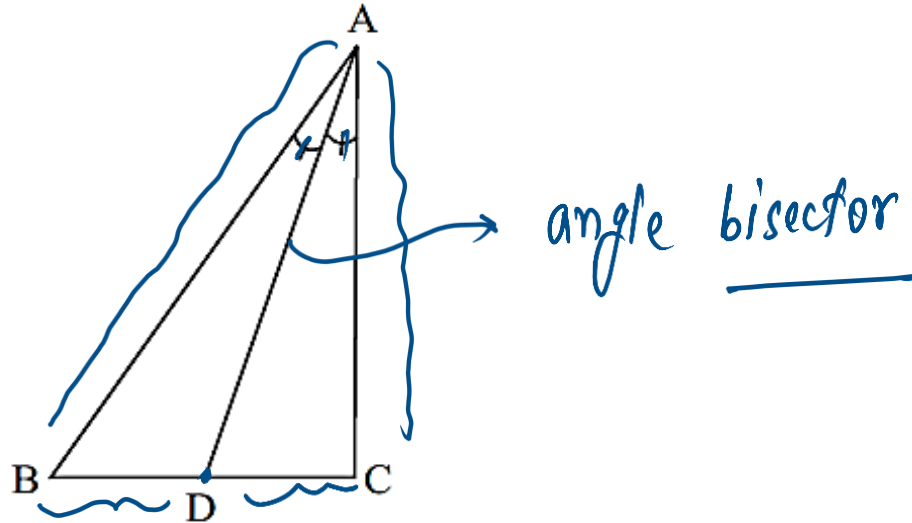
DE is parallel to AB i.e. $DE \parallel AB$ and $DE = \frac{1}{2} AB$



ANGLE BISECTOR THEOREM

Bisector of an angle (internal or external) of a triangle divides the opposite side (internally or externally) in the ratio of the sides containing the angle.

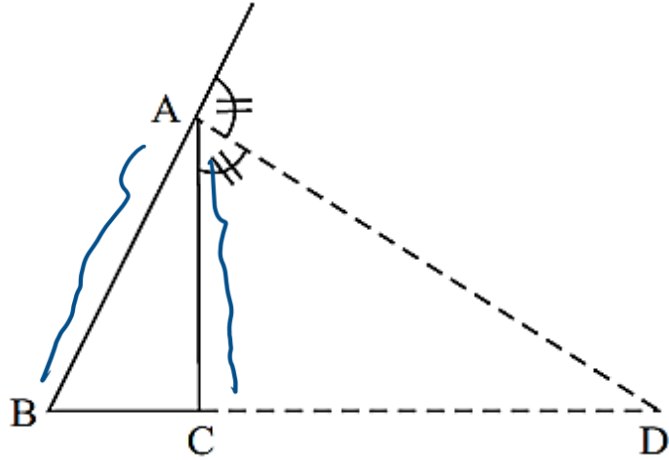
For example:



In figure AD is the bisector of exterior $\angle BAC$

$$\therefore \frac{AB}{AC} = \frac{BD}{DC}$$

ANGLE BISECTOR THEOREM



In figure AD is the bisector of exterior $\angle BAC$.

$$\therefore \frac{AB}{AC} = \frac{BD}{DC} \checkmark$$

Converse of the angle bisector theorem is also true.

MEDIAN & CENTROID

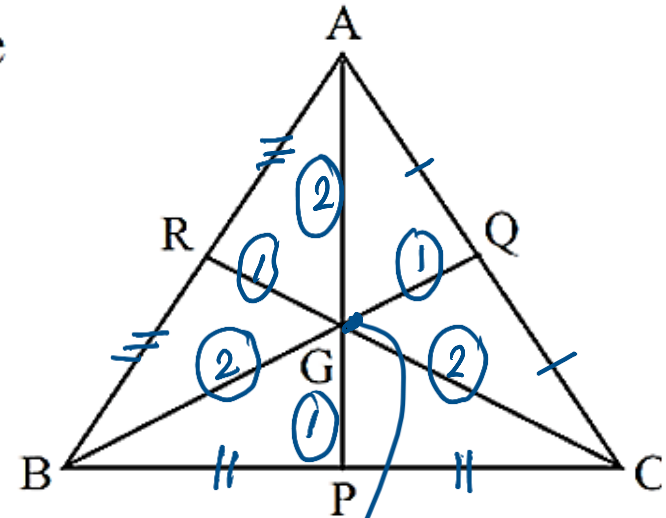
We know that a line segment joining the mid point of a side of a triangle to its opposite vertex is called a median.

AP , BQ and CR are medians of $\triangle ABC$ where P , Q and R are mid points of sides BC , CA and AB respectively.

(i) Three medians of a triangle are concurrent. The point of concurrent of three medians is called Centroid of the triangle denoted by G .

(ii) Centroid of the triangle divides each median in the ratio $2 : 1$

i.e. $\underline{AG : GP} = \underline{BG : GQ} = \underline{CG : GR} = 2 : 1$, where G is the centroid of $\triangle ABC$.



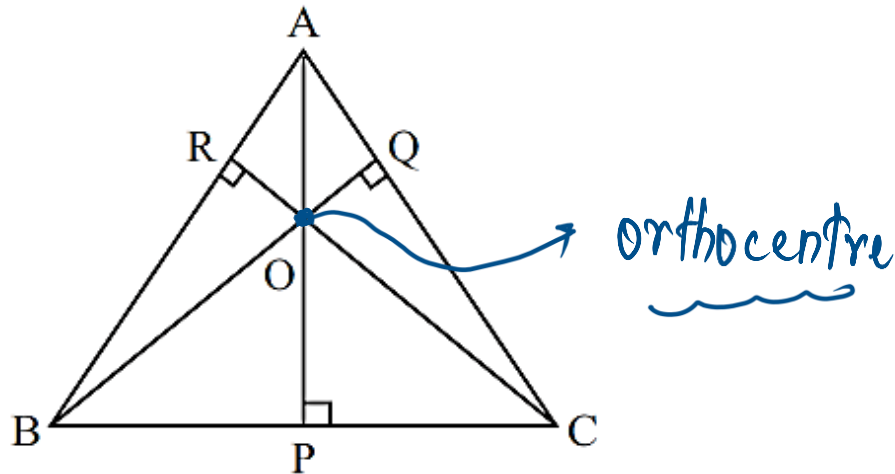
point of intersection
of medians

(centroid)

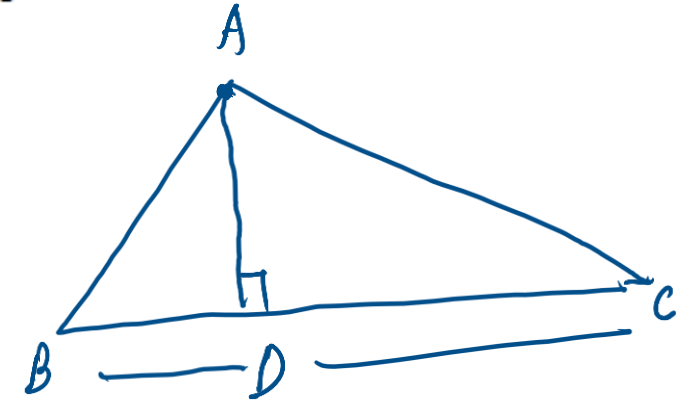
ALTITUDE & ORTHOCENTRE

A perpendicular drawn from any vertex of a triangle to its opposite side is called altitude of the triangle. There are three altitudes of a triangle.

In the figure, AP , BQ and CR are altitudes of $\triangle ABC$. The altitudes of a triangle are concurrent (meet at a point) and the point of concurrency of altitudes is called Ortho-centre of the triangle, denoted by O .



In figure, AP , BQ and CR meet at O , hence O is the orthocentre of the triangle ABC . ✓



(AD is the altitude for BC)

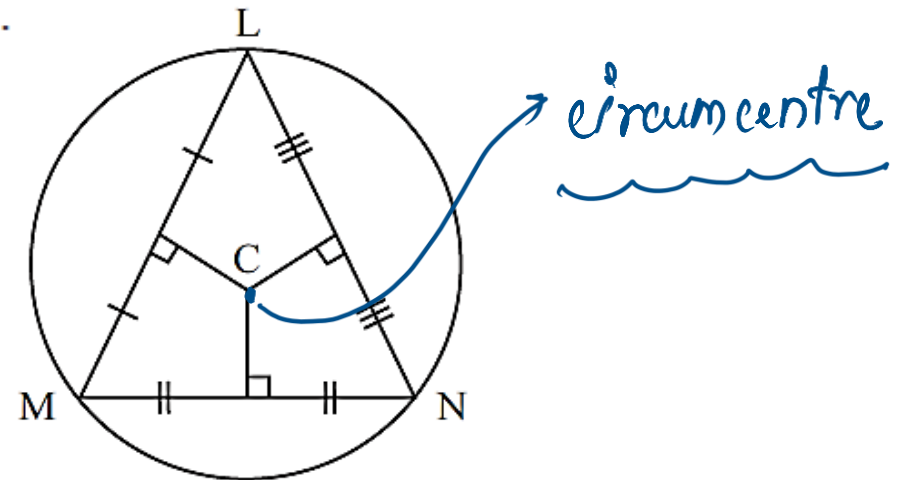
PERPENDICULAR BISECTOR & CIRCUMCENTRE

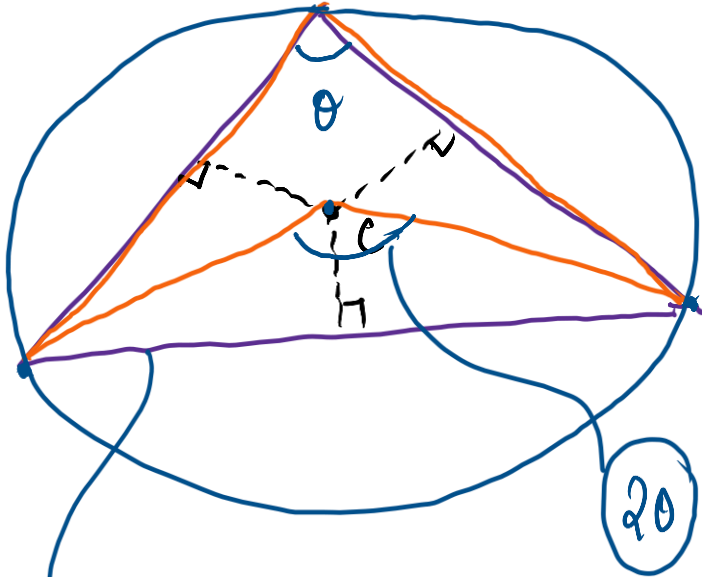
A line which is perpendicular to a side of a triangle and also bisects the side is called a perpendicular bisector of the side.

- (i) Perpendicular bisectors of sides of a triangle are concurrent and the point of concurrency is called circumcentre of the triangle, denoted by 'C'.
- (ii) The circumcentre of a triangle is centre of the circle that circumscribes the triangle.
- (iii) Angle formed by any side of the triangle at the circumcentre is twice the vertical angle opposite to the side.

In figure, perpendicular bisectors of sides LM , MN and NL of $\triangle LMN$ meet at C . Hence C is the circumcentre of the triangle LMN .

$$\angle MCN = 2 \angle MLN.$$



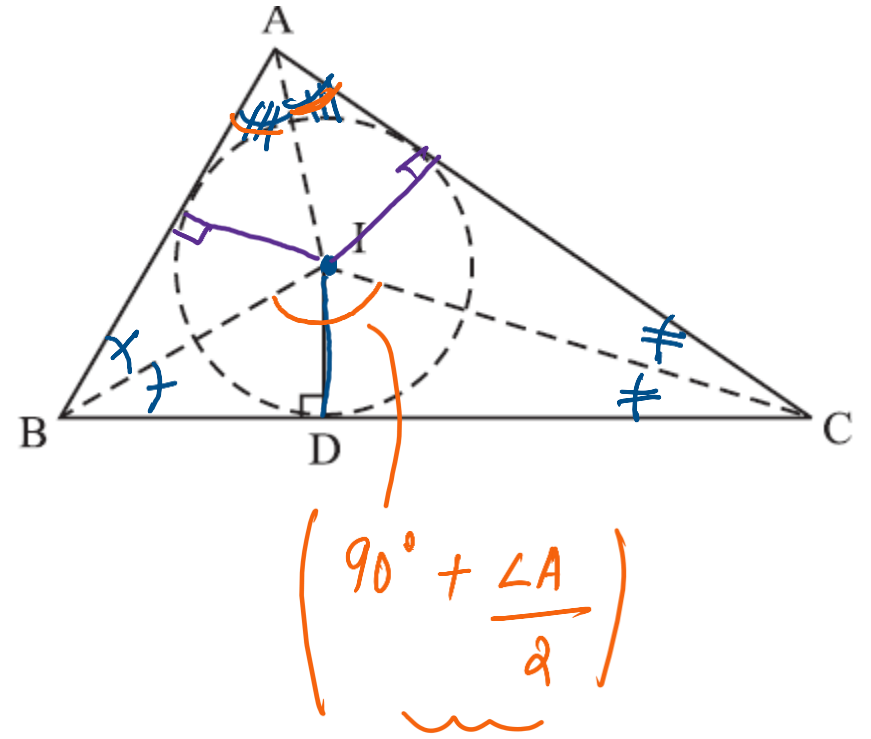


chord for circle

ANGLE BISECTOR & INCENTRE

Lines bisecting the interior angles of a triangle are called angle bisectors of triangle.

- (i) Angle bisectors of a triangle are concurrent and the point of concurrency is called Incentre of the triangle, denoted by I .
- (ii) With I as centre and radius equal to length of the perpendicular drawn from I to any side, a circle can be drawn touching the three sides of the triangle. So this is called incircle of the triangle. Incentre is equidistant from all the sides of the triangle.
- (iii) Angle formed by any side at the incentre is always 90° more than half the vertex angle opposite to the side.



IMPORTANT RESULT

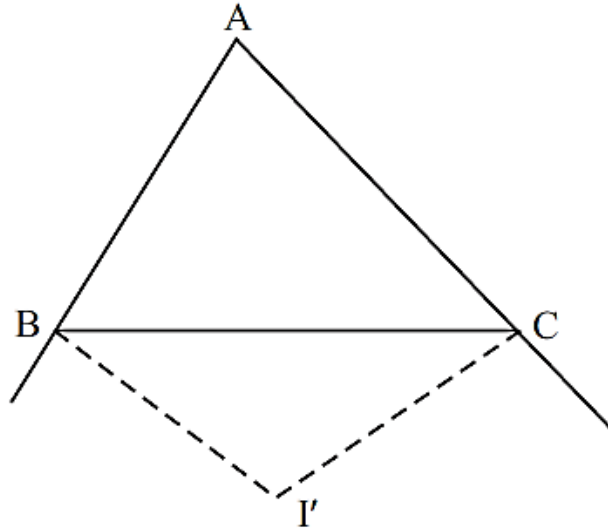
In figure AI, BI, CI are angle bisectors of $\triangle ABC$.

Hence I is the incentre of the $\triangle ABC$ and

$$\angle BIC = 90^\circ + \frac{1}{2} \angle A, \angle AIC = 90^\circ + \frac{1}{2} \angle B$$

and

$$\angle AIB = 90^\circ + \frac{1}{2} \angle C$$

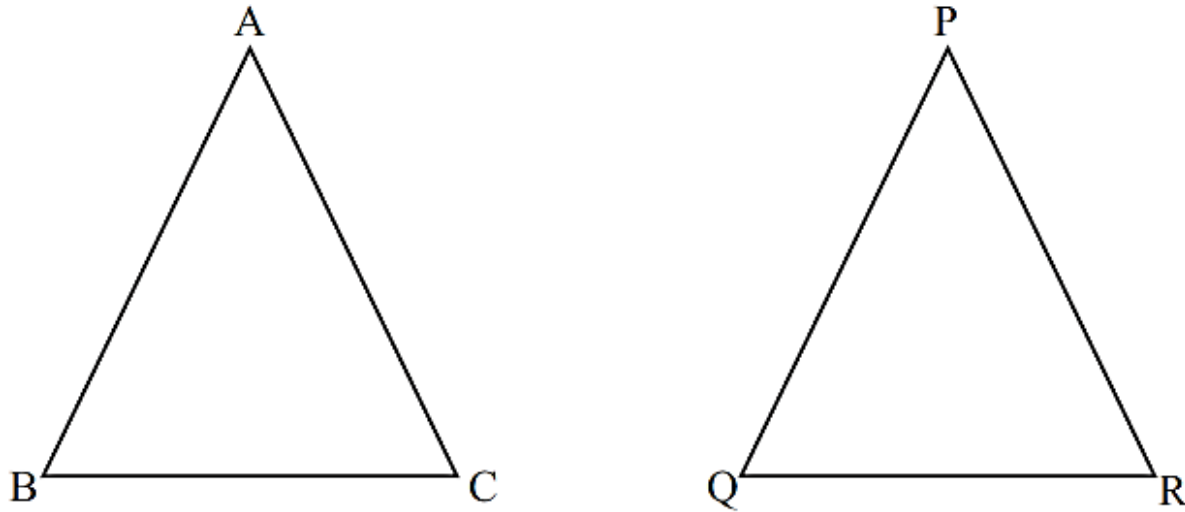


If BI' and CI' be the angle bisectors of exterior angles at B and C , then

$$\angle BI'C = 90^\circ - \frac{1}{2} \angle A.$$

CONGRUENCY OF TRIANGLE

Two triangles are congruent if they are of the same shape and size i.e. if any one of them can be made to superpose on the other it will cover exactly.



If two triangles ABC and PQR are congruent then 6 elements (i.e. three sides and three angles) of one triangle are equal to corresponding 6 elements of other triangle.

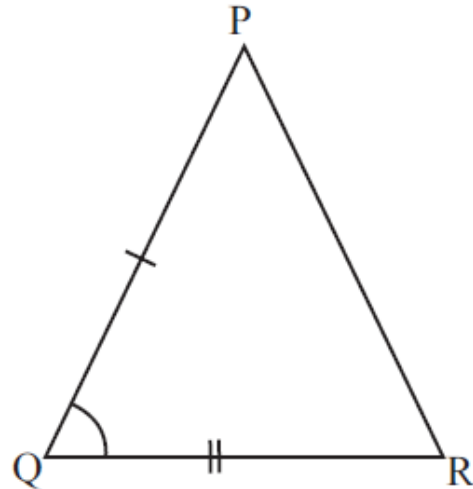
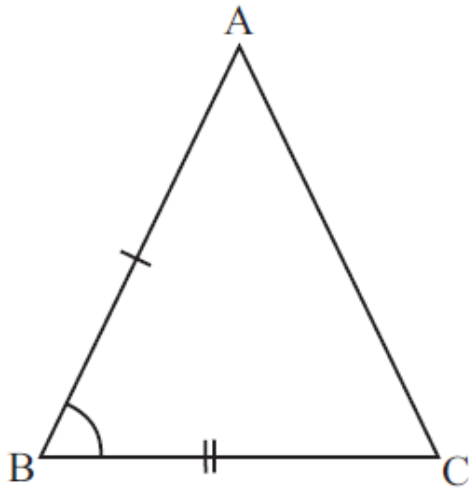
(i) $\angle A = \angle P, \angle B = \angle Q, \angle C = \angle R$

(ii) $AB = PQ, BC = QR, AC = PR$

This is symbolically written as $\triangle ABC \cong \triangle PQR$

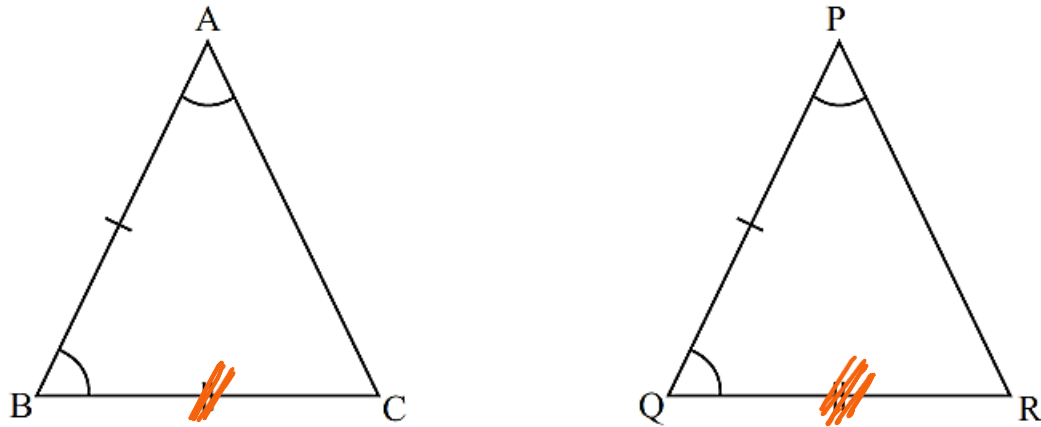
CONDITIONS OF CONGRUENCY

1. **SAS (Side-Angle-Side) Congruency:** If two sides and the included angle between these two sides of one triangle is equal to corresponding two sides and included angle between these two sides of another triangle, then the two triangles are congruent.



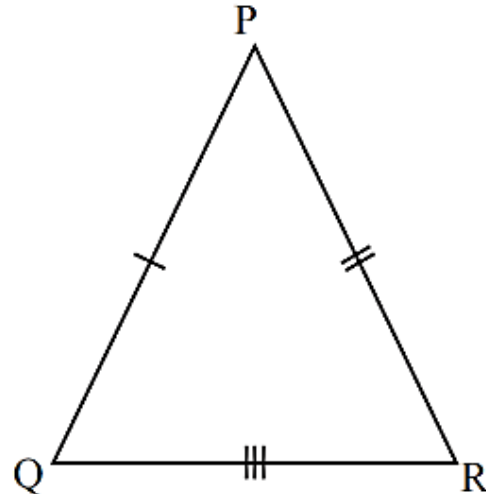
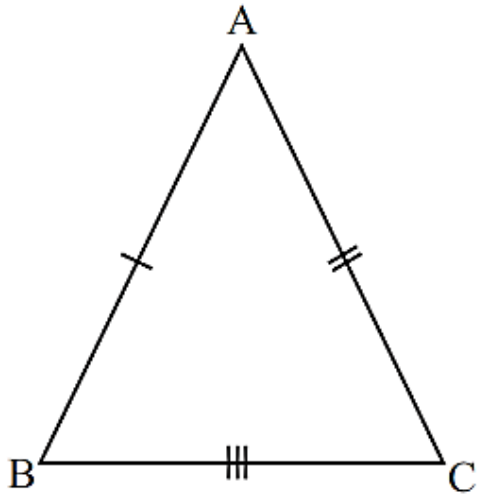
CONDITIONS OF CONGRUENCY

2. **ASA (Angle-Side-Angle) Congruency:** If two angles and included side between these two angles of one triangle are equal to corresponding angles and included side between these two angles of another triangle, then two triangles are congruent.



CONDITIONS OF CONGRUENCY

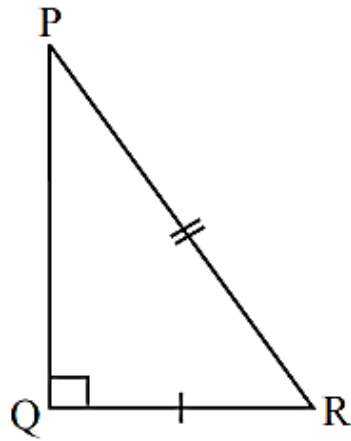
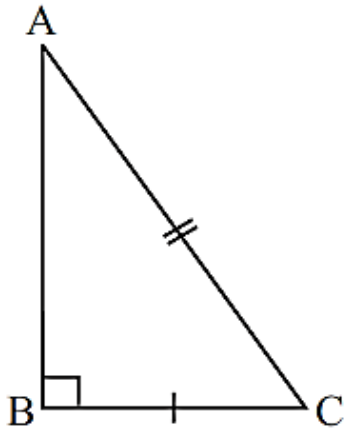
3. **SSS (Side-Side-Side) Congruency:** If three sides of one triangle are equal to corresponding three sides of another triangle, the two triangles are congruent.



CONDITIONS OF CONGRUENCY

4. RHS (Rightangle-Hypotenuse-Side) Congruency:

Two right angled triangles are congruent to each other if hypotenuse and one side of one triangle are equal to hypotenuse and corresponding side of another triangle.



SIMILARITY

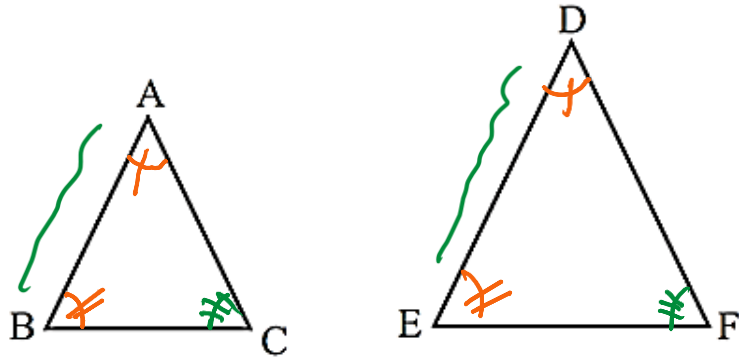
Two triangles are said to be similar, if their shapes are the same but their size may or may not be equal.

When two triangles are similar, then

- (i) all the corresponding angles are equal and
- (ii) all the corresponding sides are in the same ratio (or proportion)

SIMILARITY

In two similar triangles, sides opposite to equal angles are called corresponding sides. And angles opposite to side proportional to each other are called corresponding angles.



If $\triangle ABC$ and $\triangle DEF$ are similar, then

$$\angle A = \angle D$$

$$\angle B = \angle E$$

$$\angle C = \angle F$$

$$\text{and } \frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$$

$\triangle ABC \sim \triangle DEF$, read as triangle ABC is similar to triangle DEF .

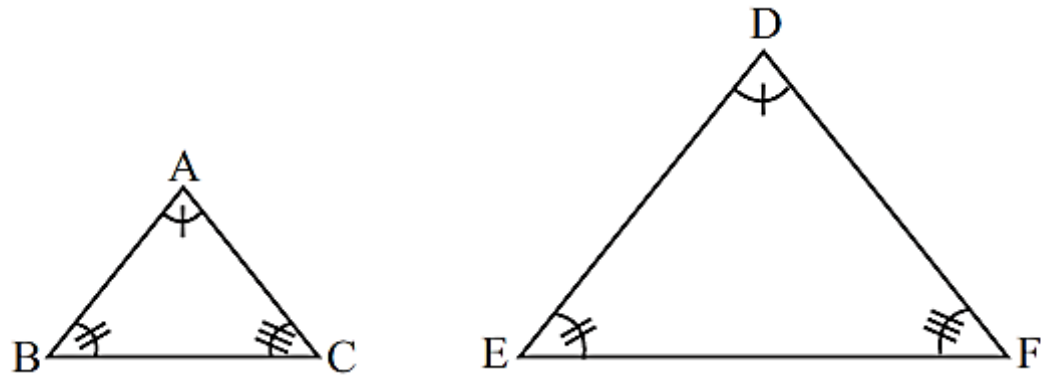
Here \sim is the sign of similarity.

congruence \cong
similar \sim

CONDITIONS OF SIMILARITY

1. AAA (Angle–Angle–Angle) Similarity: Two triangles are said to be similar, if their all corresponding angles are equal.

For example:

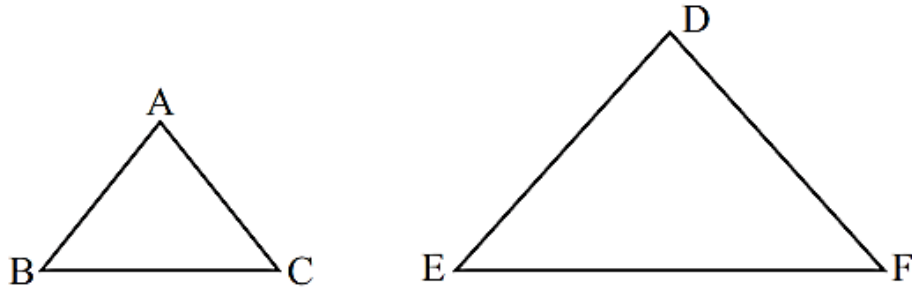


(AA) — similarity criteria (Two angles be equal)

CONDITIONS OF SIMILARITY

2. **SSS (Side–Side–Side) Similarity:** Two triangles are said to be similar, if sides of one triangle are proportional (or in the same ratio of) to the sides of the other triangle:

For example:



In $\triangle ABC$ and $\triangle DEF$, if

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD} \quad \checkmark \quad (\text{sides be proportional})$$

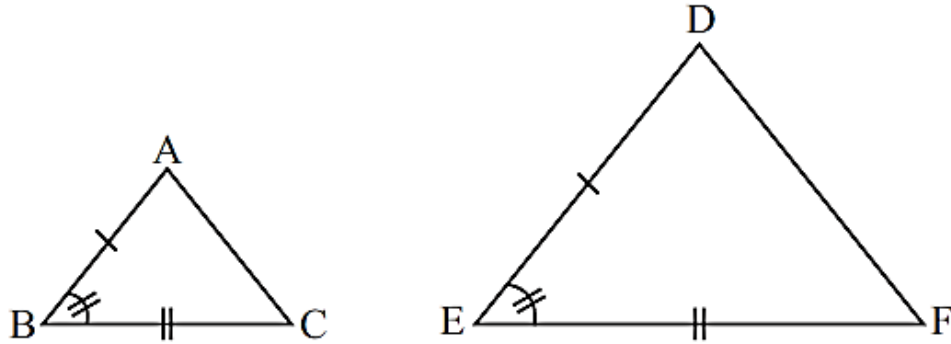
Then $\triangle ABC \sim \triangle DEF$ [By SSS Similarity]



CONDITIONS OF SIMILARITY

3. **SAS (Side–Angle–Side) Similarity:** Two triangles are said to be similar if two sides of a triangle are proportional to the two sides of the other triangle and the angles included between these sides of two triangles are equal.

For example:



In $\triangle ABC$ and $\triangle DEF$, if

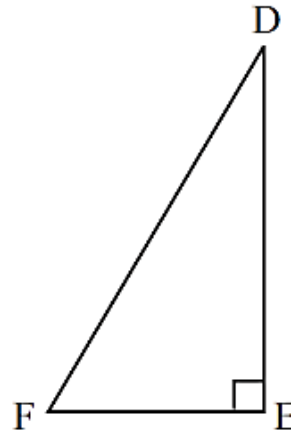
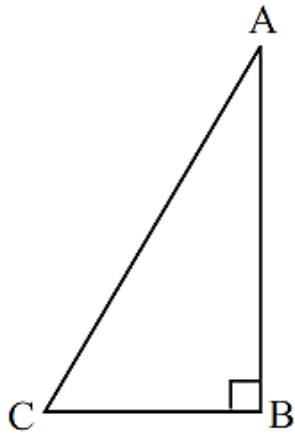
$$\frac{AB}{DE} = \frac{BC}{EF}$$

and $\angle B = \angle E$

Then, $\triangle ABC \sim \triangle DEF$ [By SAS Similarity]

CONDITIONS OF SIMILARITY

4. **RHS (Rightangle-Hypotenuse-Side) Similarity:** Two triangles are said to be similar if one angle of both triangle is right angle and hypotenuse of both triangles are proportional to any one other side of both triangles respectively.



In $\triangle ABC$ and $\triangle DEF$, if

$$\angle B = \angle E [= 90^\circ]$$

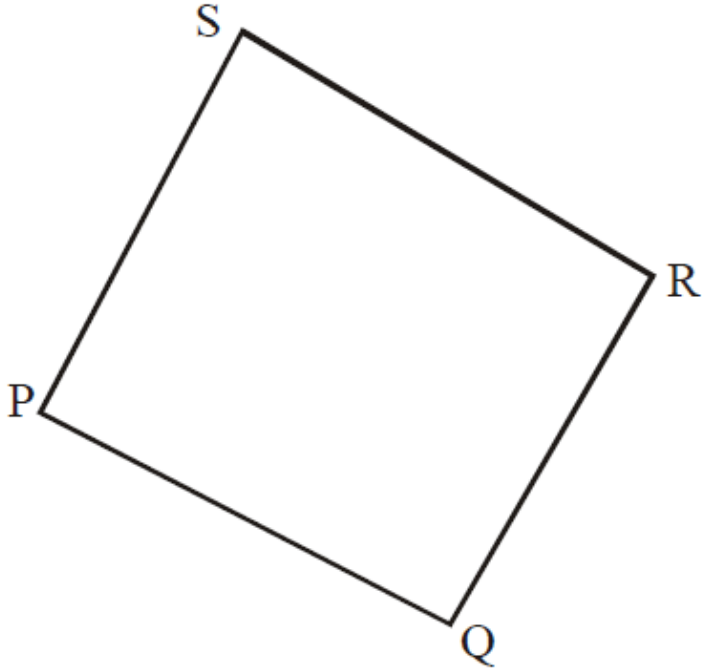
$$\frac{AC}{DF} = \frac{AB}{DE}$$

Then $\triangle ABC \sim \triangle DEF$ [By RHS similarity]

hypotenuse ratio = any leg ratio

QUADRILATERAL

A figure formed by joining four points is called a quadrilateral.
A quadrilateral has four sides, four angles and four vertices.

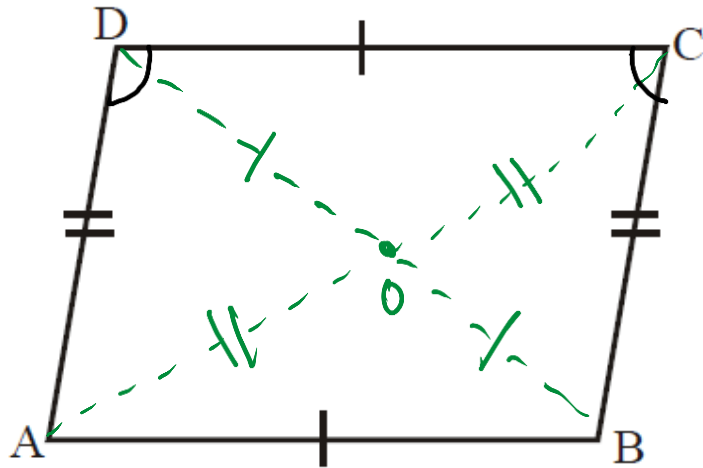


In quadrilateral PQRS, PQ, QR, RS and SP are the four sides; P, Q, R and S are four vertices and $\angle P$, $\angle Q$, $\angle R$ and $\angle S$ are the four angles.

- The sum of the angles of a quadrilateral is 360° .
 $\angle P + \angle Q + \angle R + \angle S = 360^\circ$

TYPES OF QUADRILATERAL

Parallelogram : A quadrilateral whose opposite sides are parallel is called parallelogram.

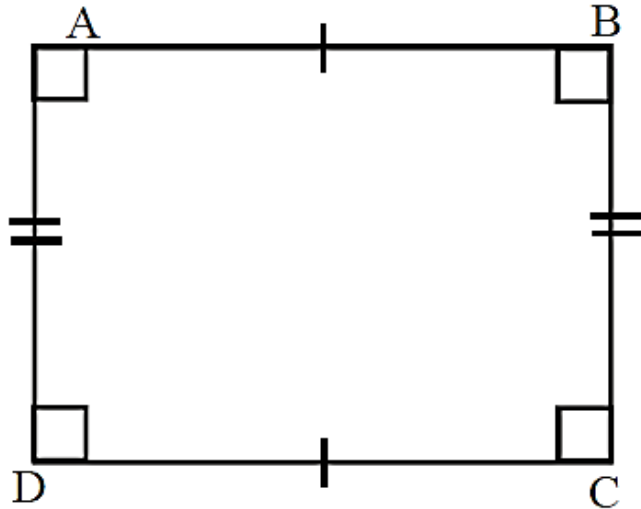


Properties :

- (i) Opposite sides are parallel and equal.
- (ii) Opposite angles are equal.
- (iii) Diagonals bisect each other.
- (iv) Sum of any two adjacent angles is 180° . $\longrightarrow \angle C + \angle D = 180^\circ$
- (v) Each diagonal divides the parallelogram into two triangles of equal area.

TYPES OF QUADRILATERAL

Rectangle : A parallelogram, in which each angle is a right angle, i.e., 90° is called a rectangle.

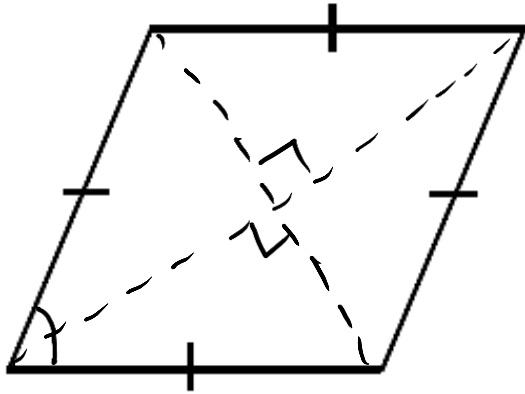


Properties :

- (i) Opposite sides are parallel and equal.
- (ii) Each angle is equal to 90° .
- (iii) Diagonals are equal and bisect each other.

TYPES OF QUADRILATERAL

Rhombus : A parallelogram in which all sides are congruent (or equal) is called a rhombus.

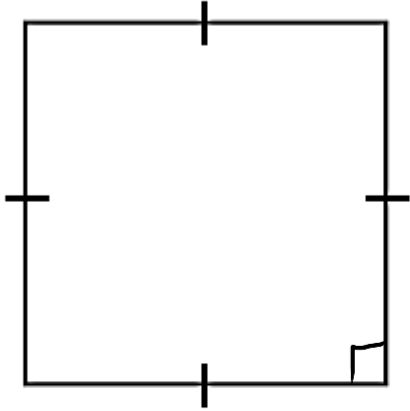


Properties :

- (i) Opposite sides are parallel.
- (ii) All sides are equal.
- (iii) Opposite angles are equal.
- (iv) Diagonals bisect each other at right angle.

TYPES OF QUADRILATERAL

Square : A rectangle in which all sides are equal is called a square.

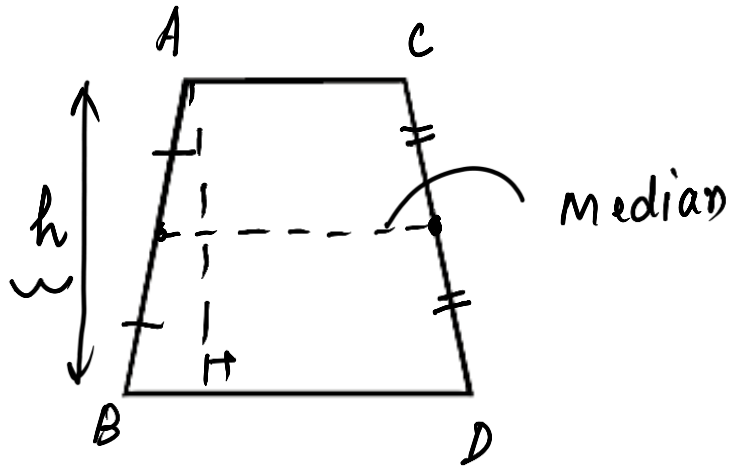


Properties :

- (i) All sides are equal and opposite sides are parallel.
- (ii) All angles are 90° .
- (iii) The diagonals are equal and bisect each other at right angle.

TYPES OF QUADRILATERAL

Trapezium : A quadrilateral is called a trapezium if two of the opposite sides are parallel but the other two sides are not parallel.



Properties :

- (i) The segment joining the mid-points of the non-parallel sides is called the median of the trapezium.

$$\left\{ \text{Median} = \frac{1}{2} \times \text{sum of the parallel sides} \right\} = \frac{1}{2} (AC + BD)$$

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