

CDS 1 2025

LIVE

MATHS

TRIGONOMETRY

CLASS 2

NAVJYOTI SIR

SSBCrack
CLAMS

Crack
EXAMS



28 Nov 2024 Live Classes Schedule

9:00AM

28 NOVEMBER 2024 DAILY DEFENCE UPDATES

DIVYANSHU SIR

NDA 1 2025 LIVE CLASSES

✓ 1:00PM

PHYSICS - REFLECTION OF LIGHT - CLASS 1

NAVJYOTI SIR

✓ 4:30PM

ENGLISH - COMMONLY USED WORDS - CLASS 2

ANURADHA MA'AM

✓ 5:30PM

MATHS - LIMITS & CONTINUITY - CLASS 1

NAVJYOTI SIR

CDS 1 2025 LIVE CLASSES

✓ 1:00PM

PHYSICS - REFLECTION OF LIGHT - CLASS 1

NAVJYOTI SIR

✓ 4:30PM

ENGLISH - COMMONLY USED WORDS - CLASS 2

ANURADHA MA'AM

✓ 7:00PM

MATHS - TRIGONOMETRY - CLASS 2

NAVJYOTI SIR



TRIGONOMETRIC FORMULAE

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\sin 75^\circ = \sin (45^\circ + 30^\circ)$$

$$= \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ$$

$$= \left(\frac{1}{\sqrt{2}}\right)\left(\frac{\sqrt{3}}{2}\right) + \left(\frac{1}{\sqrt{2}}\right)\left(\frac{1}{2}\right)$$

$$= \frac{\sqrt{3} + 1}{2\sqrt{2}}$$

TRIGONOMETRIC FORMULAE

$$\textcircled{\#} \tan (A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\textcircled{\#} \tan (A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\cot (A + B) = \frac{\cot A \cot B - 1}{\cot A + \cot B}$$

$$\cot (A - B) = \frac{\cot A \cot B - 1}{\cot B - \cot A}$$

TRIGONOMETRIC FORMULAE

$$\begin{aligned} & \sin(A + B) \sin(A - B) \\ &= \sin^2 A - \sin^2 B = \cos^2 B - \cos^2 A \\ & \cos(A + B) \cos(A - B) \\ &= \cos^2 A - \sin^2 B = \cos^2 B - \sin^2 A \end{aligned}$$

Q) Match List_I with List_II and select the correct answer using the code given below the lists

	List-I		List-II
A.	$\tan 15^\circ$	1.	$-2 - \sqrt{3}$
B.	$\tan 75^\circ$	2.	$2 + \sqrt{3}$
C.	$\tan 105^\circ$	3.	$-2 + \sqrt{3}$
		4.	$2 - \sqrt{3}$ ✓

Codes :

	A	B	C
(a)	4	1	2
✓(b)	4	2	1
(c)	3	2	1
(d)	2	1	4

$$A.) \tan 15^\circ$$

$$\tan (45^\circ - 30^\circ)$$

$$\frac{\tan 45^\circ - \tan 30^\circ}{1 + \tan 45^\circ \tan 30^\circ}$$

$$1 + \tan 45^\circ \tan 30^\circ$$

$$\frac{1 - \frac{1}{\sqrt{3}}}{1 + \frac{1}{\sqrt{3}}} = \frac{\sqrt{3}-1}{\sqrt{3}+1} \times \frac{\sqrt{3}-1}{\sqrt{3}-1}$$

$$= \frac{\sqrt{3}-1}{\sqrt{3}+1} \times \frac{\sqrt{3}-1}{\sqrt{3}-1}$$

$$= \frac{3+1-2\sqrt{3}}{2} = \frac{4-2\sqrt{3}}{2} = \underbrace{2-\sqrt{3}}$$

(*) $\tan 75^\circ = \tan(45^\circ + 30^\circ)$ or, $\tan(90^\circ - 15^\circ) = \cot 15^\circ = \frac{1}{\tan 15^\circ}$

$$= \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}} = \frac{\sqrt{3}+1}{\sqrt{3}-1} = \frac{1}{2-\sqrt{3}} = \frac{2+\sqrt{3}}{4-3} = \underline{2+\sqrt{3}}$$

$$\tan 105^\circ = \tan(180^\circ - 75^\circ) = -\tan 75^\circ = -(2+\sqrt{3}) = -2-\sqrt{3}$$

Q) Match List_I with List_II and select the correct answer using the code given below the lists

	List-I		List-II
A.	$\tan 15^\circ$	1.	$-2 - \sqrt{3}$
B.	$\tan 75^\circ$	2.	$2 + \sqrt{3}$
C.	$\tan 105^\circ$	3.	$-2 + \sqrt{3}$
		4.	$2 - \sqrt{3}$

Codes :

	A	B	C
(a)	4	1	2
(b)	4	2	1
(c)	3	2	1
(d)	2	1	4

Ans: (c)

TRIGONOMETRIC FORMULAE

$$\# \sin 2\theta = 2 \sin \theta \cos \theta = \frac{2 \tan \theta}{1 + \tan^2 \theta} \checkmark$$

$$\# \cos 2\theta = \cos^2 \theta - \sin^2 \theta = 1 - 2 \sin^2 \theta$$

$$= 2 \cos^2 \theta - 1 = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

$$\cos^2 \theta = \frac{1}{2} (1 + \cos 2\theta), \sin^2 \theta = \frac{1}{2} (1 - \cos 2\theta)$$

$$\# \tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$$

$$\cot 2\theta = \frac{\cot^2 \theta - 1}{2 \cot \theta}$$

$$\sin(\theta + \theta) = \sin \theta \cos \theta + \cos \theta \sin \theta$$

$$= \underline{2 \sin \theta \cos \theta}$$

$$\cos(\theta + \theta) = \cos \theta \cos \theta - \sin \theta \sin \theta$$

$$\textcircled{1} = \cos^2 \theta - \sin^2 \theta$$

$$\textcircled{2} = 1 - 2 \sin^2 \theta$$

$$\textcircled{3} = 2 \cos^2 \theta - 1$$

$$\textcircled{4} = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

$$\sin 2x = 2 \sin x \cos x$$

angle is halved,

$$\sin 4x = 2 \sin 2x \cos 2x$$

$$\sin x = 2 \sin \frac{x}{2} \cos \frac{x}{2}$$

(similarly for $\cos 2x$, $\tan 2x$ etc.)

Q) What is $\sqrt{2 + \sqrt{2 + \sqrt{2 + 2 \cos 4A}}}$ equal to?

- (a) $\cos A$ (b) $\cos(2A)$
 (c) $2\cos(A/2)$ (d) $\sqrt{2 \cos A}$

$$\begin{aligned} 2 + 2 \cos 4A &= 2(1 + \cos 4A) \\ &= 2(2 \cos^2 2A) \\ &= 4 \cos^2 2A \end{aligned}$$

$$\sqrt{2 + 2 \cos 4A} = \sqrt{4 \cos^2 2A} = 2 \cos 2A$$

$$\cos 4A = 1 - 2 \sin^2 2A$$

$$1 - \cos 4A = 2 \sin^2 2A$$

$$\cos 4A = 2 \cos^2 2A - 1$$

$$\cos 4A + 1 = 2 \cos^2 2A$$

$$\begin{aligned}
2 + 2 \cos 2A &= 2(1 + \cos 2A) \\
&= 2(2 \cos^2 A) \\
&= 4 \cos^2 A
\end{aligned}$$

$$\sqrt{2 + 2 \cos 2A} = \sqrt{4 \cos^2 A} = \underline{2 \cos A}$$

$$\begin{aligned}
2 + 2 \cos A &= 2(1 + \cos A) \\
&= 2\left(2 \cos^2 \frac{A}{2}\right) \\
&= 4 \cos^2 \frac{A}{2}
\end{aligned}$$

$$\left. \begin{aligned}
1 + \cos A &= 2 \cos^2 \frac{A}{2} \\
1 - \cos A &= 2 \sin^2 \frac{A}{2}
\end{aligned} \right\}$$

$$\sqrt{2 + 2 \cos A} = \sqrt{4 \cos^2 \frac{A}{2}} = \textcircled{2 \cos \frac{A}{2}}$$

Q) What is $\sqrt{2 + \sqrt{2 + \sqrt{2 + 2 \cos 4A}}}$ equal to?

- (a) $\cos A$ (b) $\cos(2A)$
(c) $2\cos(A/2)$ (d) $\sqrt{2 \cos A}$

Ans: (c)

TRIGONOMETRIC FORMULAE

$$\# \text{ (i) } \sin 3\theta = \underline{3} \sin \theta - \underline{4} \sin^3 \theta$$

$$\# \text{ (ii) } \cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$$

$$\# \text{ (iii) } \tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$$

$$\text{(iv) } \cot 3\theta = \frac{\cot^3 \theta - 3 \cot \theta}{3 \cot^2 \theta - 1} = \frac{3 \cot \theta - \cot^3 \theta}{1 - 3 \cot^2 \theta}$$

$$-2 \sin^3 \theta + \sin \theta (1 + 2 \cos^2 \theta)$$

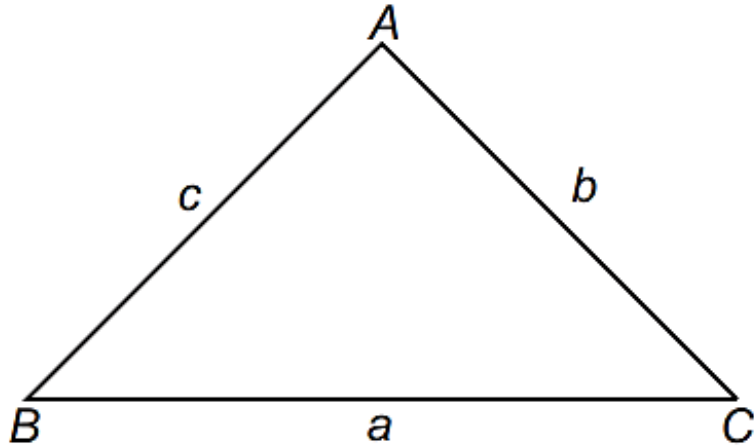
$$-2 \sin^3 \theta + \sin \theta (3 - 2 \sin^2 \theta)$$

$$\sin(\theta + 2\theta) = \sin \theta \cos 2\theta + \cos \theta \sin 2\theta = 3 \sin \theta - 4 \sin^3 \theta$$

$$= \sin \theta (1 - 2 \sin^2 \theta) + \cos \theta (2 \sin \theta \cos \theta)$$

$$= \sin \theta - 2 \sin^3 \theta + 2 \sin \theta \cos^2 \theta$$

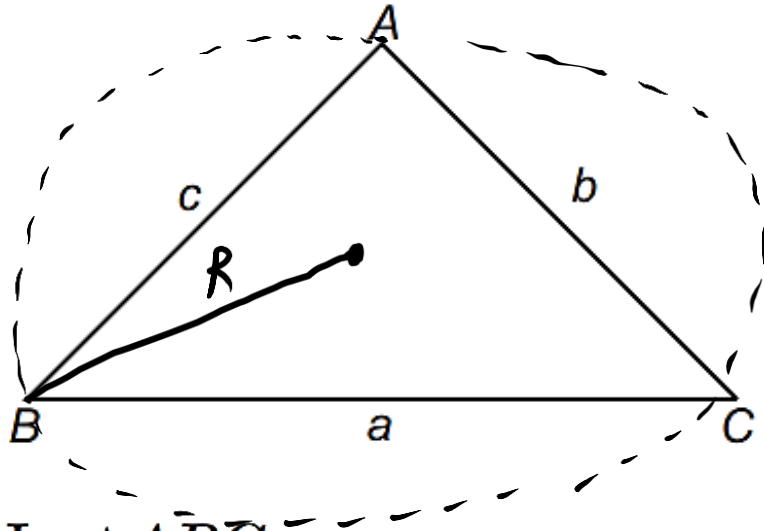
RELATION BETWEEN SIDES AND ANGLE



In a $\triangle ABC$ the length of sides opposite to the angles A , B and C are denoted by a , b and c . Area of a triangle and perimeter of a triangle are denoted by Δ and $2s$, respectively and

$$s = \frac{a + b + c}{2}$$

SINE RULE



In $\triangle ABC$,

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c} = \frac{1}{2R} \quad \left\{ \begin{array}{l} \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R \end{array} \right.$$

where, R be the radius of circumcircle of the $\triangle ABC$.

EXAMPLE

In a $\triangle ABC$, $A = 30^\circ$, $b = 8$, $a = 6$, then
 $B = \sin^{-1} x$, where x is equal to

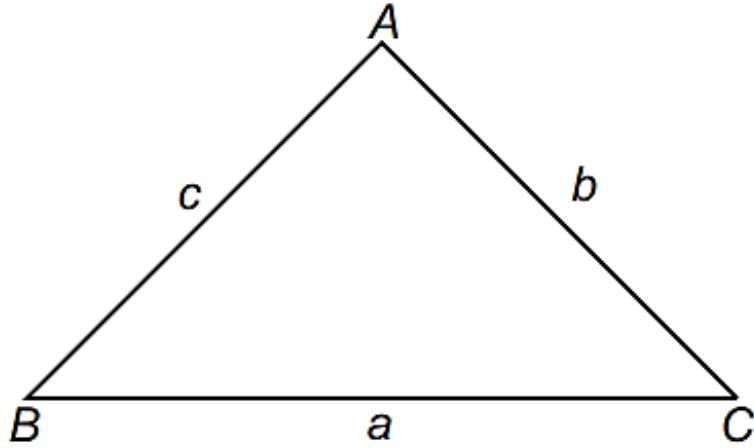
(a) $\frac{1}{2}$
✓ (c) $\frac{2}{3}$

(b) $\frac{1}{3}$
(d) 1

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{6}{\sin 30^\circ} = \frac{8}{\sin B} \Rightarrow \sin B = \frac{4}{6} = \frac{2}{3} \Rightarrow B = \sin^{-1} \left(\frac{2}{3} \right)$$

COSINE RULE



In $\triangle ABC$,

$$1. \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

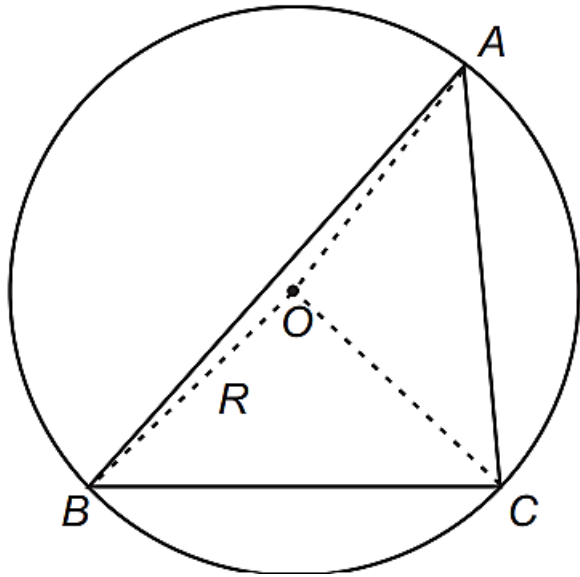
$$2. \cos B = \frac{a^2 + c^2 - b^2}{2ca}$$

$$3. \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

In $\triangle ABC$,

- If $\angle A = 60^\circ$, then $b^2 + c^2 - a^2 = bc$
- If $\angle B = 60^\circ$, then $a^2 + c^2 - b^2 = ac$
- If $\angle C = 60^\circ$, then $a^2 + b^2 - c^2 = ab$

CIRCUMCIRCLE



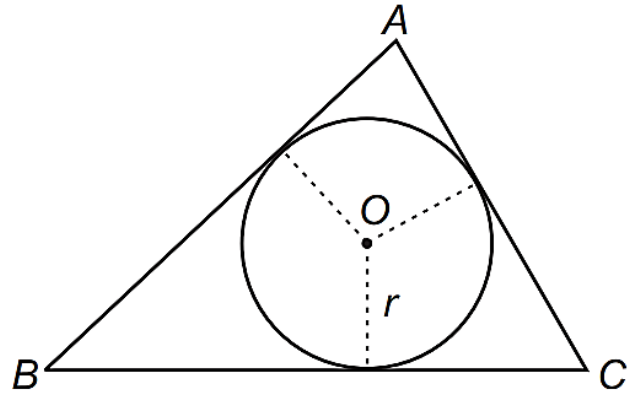
$$1. R = \frac{a}{2 \sin A}$$

$$3. R = \frac{c}{2 \sin C}$$

$$2. R = \frac{b}{2 \sin B}$$

$$4. R = \frac{abc}{4\Delta} \rightarrow (\text{area of triangle})$$

INCIRCLE



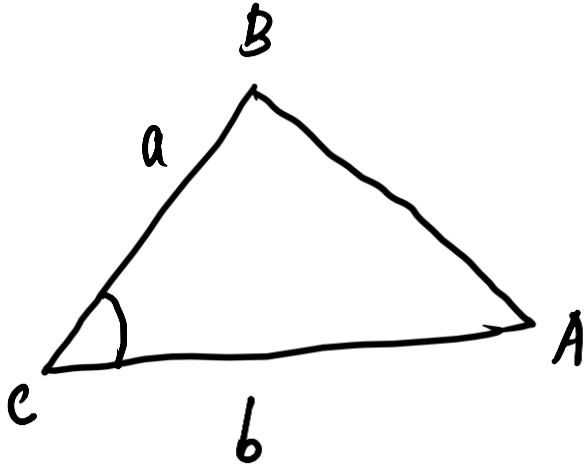
$$r = \frac{\Delta}{s}$$

AREA OF TRIANGLE

$$1. \Delta = \frac{1}{2} ab \sin C$$

$$2. \Delta = \frac{1}{2} bc \sin A$$

$$3. \Delta = \frac{1}{2} ca \sin B$$



length of two sides and angle included between them.

EXAMPLE

In a ΔABC , if $a = 2x$, $b = 2y$ and $\angle C = 120^\circ$, then the area of the triangle is

(a) xy

(b) $xy\sqrt{3}$

(c) $3xy$

(d) $2xy$

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