

NDA 1 2025

LIVE

MATHS

PERMUTATION & COMBINATION

CLASS 1



NAVJYOTI SIR

Crack
EXAMS



6 Nov 2024 Live Classes Schedule

8:00AM -- 06 NOVEMBER 2024 DAILY CURRENT AFFAIRS RUBY MA'AM

9:00AM -- 06 NOVEMBER 2024 DAILY DEFENCE UPDATES DIVYANSHU SIR

SSB INTERVIEW LIVE CLASSES

9:30AM -- OVERVIEW OF OIR & PRACTICE ANURADHA MA'AM

NDA 1 2025 LIVE CLASSES

11:30AM -- GK - MEDIEVAL HISTORY - CLASS 2 RUBY MA'AM

1:00PM -- CHEMISTRY MCQ - CLASS 4 SHIVANGI MA'AM

4:00PM -- MATHS - PERMUTATION & COMBINATION - CLASS 1 NAVJYOTI SIR

✓ 5:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM

CDS 1 2025 LIVE CLASSES

11:30AM -- GK - MEDIEVAL HISTORY - CLASS 2 RUBY MA'AM

1:00PM -- CHEMISTRY MCQ - CLASS 4 SHIVANGI MA'AM

5:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM

✓ 7:00PM -- MATHS - GEOMETRY - CLASS 2 NAVJYOTI SIR

AFCAT 1 2025 LIVE CLASSES

✓ 4:00PM -- STATIC GK - COUNTRY CAPITAL CURRENCY - CLASS 2 DIVYANSHU SIR

5:30PM -- ENGLISH - ORDERING OF SENTENCES - CLASS 1 ANURADHA MA'AM



FACTORIAL

$$n! \quad \text{or} \quad \underline{n} = n \times (n-1) \times (n-2) \times \dots \times 1$$

$$6! = 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720$$

$$4! = 4 \times 3 \times 2 \times 1 = 24$$

$$\left| \begin{array}{l} 1! = 1 \\ 2! = 2 \times 1 = 2 \\ 3! = 3 \times 2 \times 1 = 6 \end{array} \right.$$

$$4! = 24$$

$$5! = 120$$

$$6! = 720$$

FACTORIAL

→ Factorial is defined for whole numbers.

$$0! = 1$$

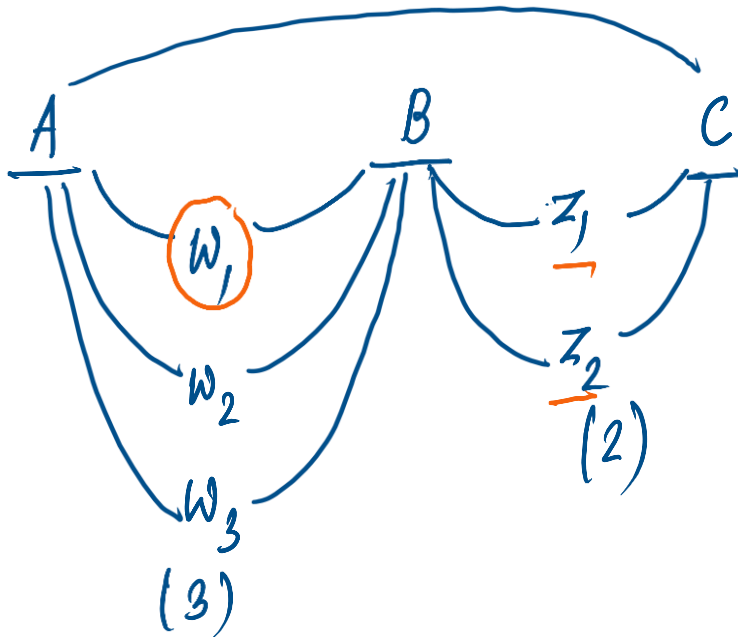
$$\begin{aligned} \rightarrow 6! &= 6 \times 5 \times 4 \times 3 \times 2 \times 1 \\ &= 6 \times 5! \\ &= 6 \times 5 \times 4! \end{aligned}$$

$$\begin{aligned} n! &= n \cdot (n-1)! \\ &= n(n-1)(n-2)! \end{aligned}$$

FUNDAMENTAL PRINCIPLE OF COUNTING

Multiplication Principle

Suppose an event E can occur in m different ways and associated with each way of occurring of E, another event F can occur in n different ways, then the total number of occurrence of the two events in the given order is $m \times n$.



Total ways of reaching C from A

$$3 \times 2 = \underline{6 \text{ ways}}$$

FUNDAMENTAL PRINCIPLE OF COUNTING

Addition Principle

If an event E can occur in m ways and another event F can occur in n ways, suppose that both can not occur together, then E or F can occur in $m + n$ ways.

EXAMPLE

In a class, there are 27 boys and 14 girls. The teacher wants to select 1 boy and 1 girl to represent the class for a function. In how many ways can the teacher make this selection?

$$27 \times 14 =$$

EXAMPLE

- (i) How many numbers are there between 99 and 1000 having 7 in the units place?
- (ii) How many numbers are there between 99 and 1000 having at least one of their digits 7?

$99 - 1000 \longrightarrow$ all will be 3-digit.

$$(i) \quad \begin{array}{c} \overset{0}{9} \\ (H) \end{array} \quad \begin{array}{c} \overset{10}{10} \\ (T) \end{array} \quad \begin{array}{c} \overset{1}{1} \\ (U) \end{array} = 9 \times 10 \times 1 = \underline{\underline{90 \text{ ways}}}$$

↓
(0-9)

(ii) Total numbers possible - numbers having no digit as 7.

(ii) Total numbers possible - Numbers having no digit as 7

$$\underline{9} \quad \underline{10} \quad \underline{10}$$

$$\underline{\underline{8}} \quad \underline{9} \quad \underline{9}$$

$$9 \times 10 \times 10 - 8 \times 9 \times 9$$

$$900 - 648 = 252$$

PERMUTATIONS

Any arrangement of some or all the things out of a given number of things in a definite order is called a permutation.

3 objects, taken 2 at a time to be arranged,

a b c

| a b
b a
b c
c b

c a
a c

(6)

Number of permutations of 'n' objects taken r at a time :

$${}^n P_r = \frac{n!}{(n-r)!} ; 0 < r \leq n$$

$${}^6 P_3 = \frac{6!}{(6-3)!} = \frac{6!}{3!} = \frac{6 \times 5 \times 4 \times \cancel{3!}}{\cancel{3!}} = \underbrace{6 \times 5 \times 4}$$

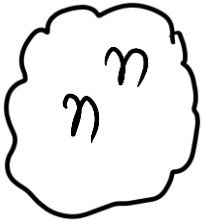
$${}^7P_2 = \frac{7!}{(7-2)!} = \frac{7!}{5!} = \frac{7 \times 6 \times \cancel{5!}}{\cancel{5!}} = \boxed{7 \times 6}$$

$${}^n P_r = \underbrace{n(n-1)(n-2)\dots(n-r+1)}_{(r \text{ nos.})}$$

PERMUTATIONS OF n OBJECTS TAKEN n

AT A TIME

Repetition Allowed



Repetition not Allowed

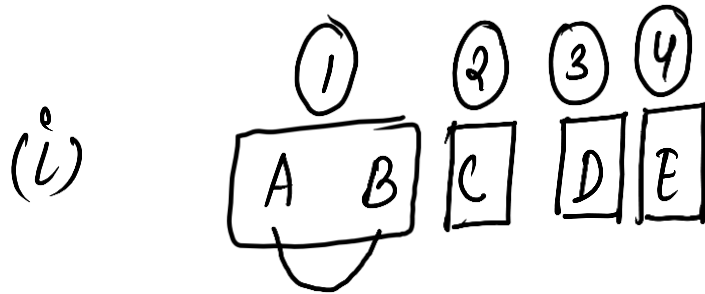
$$n(n-1) \dots 1$$

$$= n!$$

EXAMPLE

In how many ways can 5 children be arranged in a line such that

- (i) two particular children of them are always together
 (ii) two particular children of them are never together.

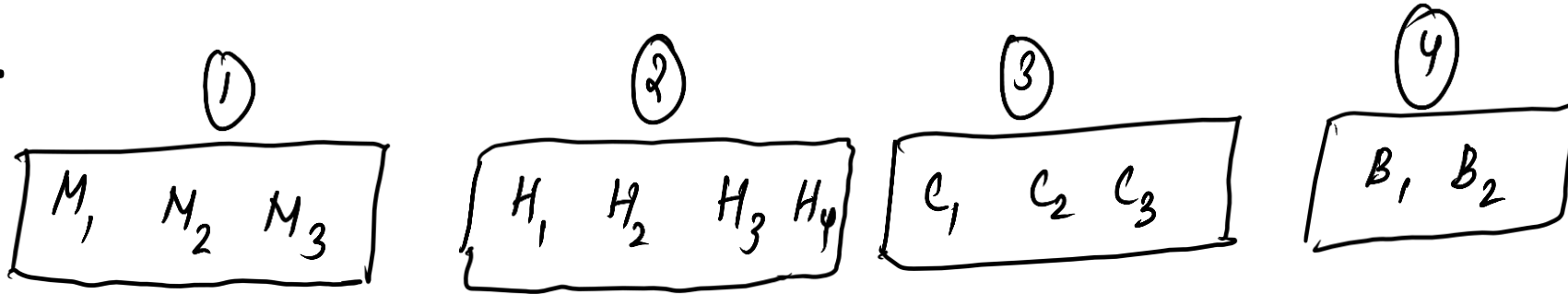


$$4! \times 2! = 24 \times 2 = 48$$

(ii) Total permutations — together = $5! - 48$
 permutations = $120 - 48$
 = 72

EXAMPLE

In how many ways 3 mathematics books, 4 history books, 3 chemistry books and 2 biology books can be arranged on a shelf so that all books of the same subjects are together.



$$4! \times 3! \times 4! \times 3! \times 2!$$

(4 groups)

PERMUTATIONS WHEN OBJECTS ARE NOT DISTINCT

The number of permutations of n objects of which p_1 are of one kind, p_2 are of second kind, ..., p_k are of k th kind and the rest if any, are of different kinds is

$$\frac{n!}{p_1! p_2! \dots p_k!}$$

EXAMPLE

If all permutations of the letters of the word **AGAIN** are arranged in the order as in a dictionary. What is the 49th word?

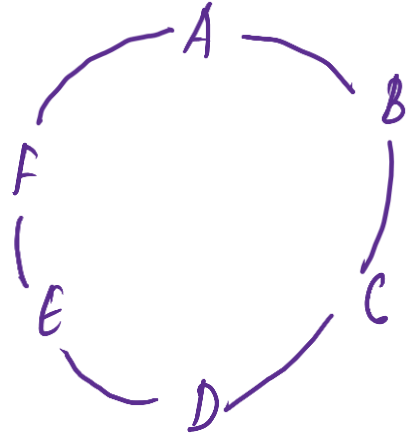
A G A I N

(A) GA I N $\rightarrow \frac{4!}{1!} = 24 \text{ words}$
 (G) AA I N $\rightarrow \frac{4!}{2!} = \frac{24}{2} = 12 \text{ words}$
 (I) AA G N $\rightarrow \frac{4!}{2!} = \frac{24}{2} = 12 \text{ words}$

$24 + 12 = 36 \text{ words}$
 $36 + 12 = 48 \text{ words}$

49th word \rightarrow will start with N \rightarrow **NAAGI**

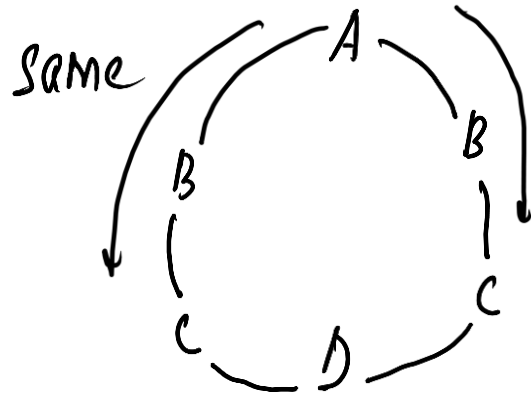
CIRCULAR PERMUTATIONS



for n objects,



$$(n-1)!$$



same

$$\frac{1}{2} (n-1)!$$

NUMBER OF PERMUTATIONS UNDER CERTAIN CONDITIONS

The number of permutation of n different things taken all together when r particular things are to be place at some r given places = $\underline{\underline{n-r}}P_{\underline{\underline{n-r}}} = \underline{\underline{(n-r)!}}$

The number of permutations of n different things taken r at a time when m particular things are to be placed at m given places = $\underline{\underline{n-m}}P_{\underline{\underline{r-m}}}$.

NUMBER OF PERMUTATIONS UNDER CERTAIN CONDITIONS

Number of permutations of n different things, taken r at a time, when a particular thing is to be always included in each arrangement, is $r \cdot {}^{n-1}P_{r-1}$



Number of permutation of n different things, taken r at a time, when m particular thing is never taken in each arrangement is ${}^{n-m}P_r$

NUMBER OF PERMUTATIONS UNDER CERTAIN CONDITIONS

Number of permutations of n different things, taken all at a time, when m specified things always come together is $m! \times (n - m + 1)!$

Number of permutations of n different things, taken all at a time, when m specified things never come together is $n! - m! \times (n - m + 1)!$

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CLASS 2



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